

A machine learning tutorial: applications of the Bioconductor MLInterfaces package to gene expression data

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1 Overview

The term *machine learning* refers to a family of computational methods for analyzing multivariate datasets. Each data point has a vector of *features* in a shared *feature space*, and may have a *class label* from some fixed finite set.

Supervised learning refers to processes that help articulate rules that map *feature vectors* to *class labels*. The class labels are known and function as supervisory information to guide rule construction. *Unsupervised learning* refers to processes that discover structure in collections of feature vectors. Typically the structure consists of a grouping of objects into clusters.

This practical introduction to machine learning will begin with a survey of a low-dimensional dataset to fix concepts, and will then address problems coming from genomic data analysis, using RNA expression and chromatin state data.

Some basic points to consider at the start:

- Distinguish predictive modeling from inference on model parameters. Typical work in epidemiology focuses on estimation of relative risks, and random samples are not required. Typical work with machine learning tools targets estimation (and minimization) of the misclassification rate. Representative samples are required for this task.
- “Two cultures”: model fitters vs. algorithmic predictors. If statistical models are correct, parameter estimation based on the mass of data can yield optimal discriminators (e.g., LDA). Algorithmic discriminators tend to prefer to identify boundary cases and downweight the mass of data (e.g., boosting, svm).
- Different learning tools have different capabilities. There is little *a priori* guidance on matching learning algorithms to aspects of problems. While it is convenient to sift through a variety of approaches, one must pay a price for the model search.
- Data and model/learner visualization are important, but visualization of higher dimensional data structures is hard. Dynamic graphics can help; look at ggobi and Rggobi for this.
- These notes provide very little mathematical background on the methods; see for example Ripley (*Pattern recognition and neural networks*, 1995), Duda, Hart, Stork (*Pattern classification*), Hastie, Tibshirani and Friedman (2003, *Elements of statistical learning*) for copious background.

2 Getting acquainted with machine learning via the crabs data

2.1 Attaching and checking the data

The following steps bring the crabs data into scope and illustrate aspects of its structure.

```
> library("MASS")
> data("crabs")
> dim(crabs)

[1] 200    8

> crabs[1:4,]

  sp sex index  FL  RW  CL  CW  BD
1  B  M     1  8.1 6.7 16.1 19.0 7.0
2  B  M     2  8.8 7.7 18.1 20.8 7.4
3  B  M     3  9.2 7.8 19.0 22.4 7.7
4  B  M     4  9.6 7.9 20.1 23.1 8.2

> table(crabs$sex)

  F  M
100 100

> library("lattice")
> print(bwplot(RW~sp/sex, data=crabs))
```

The plot is shown in Figure 1.

We will regard these data as providing five quantitative features (FL, RW, CL, CW, BD)¹ and a pair of class labels (sex, sp=species). We may regard this as a four class problem, or as two two class problems.

2.2 A simple classifier derived by human reasoning

Our first problem does not involve any computations. If you want to write R code to solve the problem, do so, but use prose first.

- *Question 1.* On the basis of the boxplots in Figure 1, comment on the prospects for predicting species on the basis of RW. State a rule for computing the predictions. Describe how to assess the performance of your rule.

¹You may consult the manual page of `crabs` for an explanation of these abbreviations.

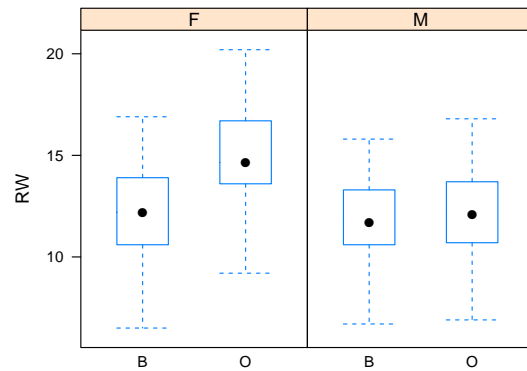


Figure 1: Boxplots of RW , the rear width in mm, stratified by species ("B" or "O" for blue or orange) and sex ("F" and "M").

2.3 Prediction via logistic regression

A simple approach to prediction involves logistic regression.

```
> m1 = glm(sp~RW, data=crabs, family=binomial)
> summary(m1)
```

Call:

```
glm(formula = sp ~ RW, family = binomial, data = crabs)
```

Deviance Residuals:

	Min	1Q	Median	3Q	Max
	-1.67807	-1.08840	-0.04168	1.07160	1.88030

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-3.44908	0.82210	-4.195	2.72e-05 ***
RW	0.27080	0.06349	4.265	2.00e-05 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance:	277.26	on 199	degrees of freedom
Residual deviance:	256.35	on 198	degrees of freedom

AIC: 260.35

Number of Fisher Scoring iterations: 4

- *Question 2.* Write down the statistical model corresponding to the R expression above. How can we derive a classifier from this model?
- *Question 3.* Perform the following computations. Discuss their interpretation. What are the estimated error rates of the two models? Is the second model, on the subset, better?

```
> plot(predict(m1,type="response"), crabs$sp)
> table(predict(m1,type="response")>.5, crabs$sp)
> m2 = update(m1, subset=(sex=="F"))
> table(predict(m2,type="response")>.5, crabs$sp[crabs$sex=="F"])
```

2.4 The cross-validation concept

Cross-validation is a technique that is widely used for reducing bias in the estimation of predictive accuracy. If no precautions are taken, bias can be caused by *overfitting* a classification algorithm to a particular dataset; the algorithm learns the classification "by heart", but performs poorly when asked to generalise it to new, unseen examples. Briefly, in cross-validation the dataset is deterministically partitioned into a series of training and test sets. The model is built for each training set and evaluated on the test set. The accuracy measures are averaged over this series of fits. Leave-one-out cross-validation consists of N fits, with N training sets of size $N-1$ and N test sets of size 1.

First let us use `MLearn` from the *MLInterfaces* package to fit a single logistic model. `MLearn` requires you to specify an index set for training. We use `c(1:30, 51:80)` to choose a training set of size 60, balanced between two species (because we know the ordering of records). This procedure also requires you to specify a probability threshold for classification. We use a typical default of 0.5. If the predicted probability of being "O" exceeds 0.5, we classify to "O", otherwise to "B".

```
> library(MLInterfaces)
> fcrabs = crabs[crabs$sex == "F", ]
> ml1 = MLearn( sp~RW, fcrabs, glmI.logistic(thresh=.5), c(1:30, 51:80),
+             family=binomial)
> ml1
```

MLInterfaces classification output container

The call was:

```
MLearn(formula = sp ~ RW, data = fcrabs, .method = glmI.logistic(thresh = 0.5),
```

```

      trainInd = c(1:30, 51:80), family = binomial)
Predicted outcome distribution for test set:
  0
40
Summary of scores on test set (use testScores() method for details):
      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
0.7553  0.8861  0.9803  0.9355  0.9917  0.9997

> confuMat(m11)

      B  0 NA
B 0 20  0
0 0 20  0

```

- *Question 4.* What does the report on `m11` tell you about predictions with this model? Can you reconcile this with the results in model `m2`? [Hint – non-randomness of the selection of the training set is a problem.]
- *Question 5.* Modify the `MLearn` call to obtain a predictor that is more successful on the test set.

Now we will illustrate cross-validation. First, we scramble the order of records in the `ExpressionSet` so that sequentially formed groups are approximately random samples.

```

> set.seed(123)
> sfcrabs = fcrabs[ sample(nrow(fcrabs)), ]

```

We invoke the `MLearn` method in two ways – first specifying a training index set, then specifying a five-fold cross-validation.

```

> sm11 = MLearn( sp~RW, sfcrabs, glmI.logistic(thresh=.5),
+   c(1:30, 51:80),
+   family=binomial)
> confuMat(sm11)

      predicted
given B  0
      B 15  6
      0  8 11

> smx1 = MLearn( sp~RW, sfcrabs, glmI.logistic(thresh=.5),
+   xvalSpec("LOG", 5, function(data, clab, iternum) {
+     which(rep(1:5, each=20) == iternum) }),
+   family=binomial)
> confuMat(smx1)

```

```

      predicted
given B  0
      B 36 14
      0 14 36

```

- *Question 6.* Define clearly the difference between models `sml1` and `smx1` and state the misclassification rate estimates associated with each model.

2.5 Exploratory multivariate analysis

2.5.1 Scatterplots

- *Question 7.* Interpret the following code, whose result is shown in Figure 2. Modify it to depict the pairwise configurations with different colors for crab genders.

```
> pairs(crabs[, -c(1:3)], col=ifelse(crabs$sp=="B", "blue", "orange"))
```

2.5.2 Principal components; biplot

Principal components analysis transforms the multivariate data X into a new coordinate system. If the original variables are X_1, \dots, X_p , then the variables in the new representation are denoted PC_1, \dots, PC_p . These new variables have the properties that PC_1 is the linear combination of the X_1, \dots, X_p having maximal variance, PC_2 is the variance-maximizing linear combination of residuals of X after projecting into the hyperplane normal to PC_1 , and so on. If most of the variation in $X_{n \times p}$ can be captured in a low dimensional linear subspace of the space spanned by the columns of X , then the scatterplots of the first few principal components give a good representation of the structure in the data.

Formally, we can compute the PC using the singular value decomposition of X , in which $X = UDV^t$, where $U_{n \times p}$ and $V_{p \times p}$ are orthonormal, and D is a diagonal matrix of p nonnegative singular values. The principal components transformation is $XV = UD$, and if D is structured so that $D_{ii} \geq D_{jj}$ whenever $i > j$, then column i of XV is PC_i . Note also that $D_{ii} = \sqrt{n-1} \text{sd}(PC_i)$.

```
> pc1 = prcomp( crabs[, -c(1:3)] )
> pairs(pc1$x, col=ifelse(crabs$sp=="B", "blue", "orange"))
```

The plot is shown in Figure 3.

The biplot, Figure 4, shows the data in PC space and also shows the relative contributions of the original variables in composing the transformation.

```
> biplot(pc1, choices=2:3, col=c("#80808080", "red"))
```

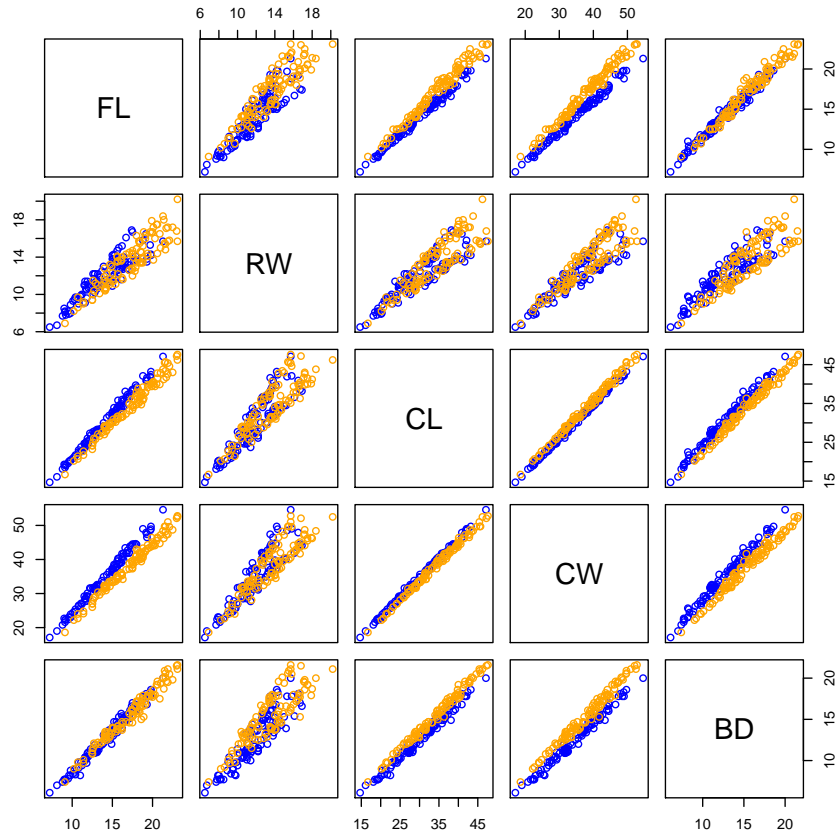


Figure 2: Pairs plot of the 5 quantitative features of the `crabs` data. Points are colored by species.

2.5.3 Clustering

A familiar technique for displaying multivariate data in high-throughput biology is called the heatmap. In this display, samples are clustered as columns, and features as rows. The clustering technique used by default is R `hclust`. This procedure builds a clustering tree for the data as follows. Distances are computed between each pair of feature vectors for all N observations. The two closest pair is joined and regarded as a new object, so there are $N - 1$ objects (clusters) at this point. This process is repeated until 1 cluster is formed; the clustering tree shows the process by which clusters are created via this agglomeration process.

The most crucial choice when applying this method is the initial choice of the distance



Figure 3: Pairs plot of the `crabs` data in principal component coordinates.

metric between the features.

Once clusters are being formed, there are several ways to measure distances between them, based on the initial between-feature distances. Single-linkage clustering takes the distance between two clusters to be the shortest distance between any two members of the different clusters; average linkage averages all the distances between members; complete-linkage uses the maximum distance between any two members of the different clusters. Other methods are also available in `hclust`.

Figure 5 shows cluster trees for samples and features. The default color choice is not great, thus we specify our own using the `col` argument. A tiled display at the top, defined via the argument `ColSideColors` shows the species codes for the samples. An important choice to be made when calling `heatmap` is the value of the argument `scale`, whose default



Figure 4: Biplot of the principal component analysis of the `crabs` data.

setting is to scale the rows, but not the columns.

```
> X = data.matrix(crabs[, -c(1:3)])
> heatmap(t(X),
+         ColSideColors=ifelse(crabs$sp=="O", "orange", "blue"),
+         col = colorRampPalette(c("blue", "white", "red"))(255))
```

Typically clustering is done in the absence of labels – it is an example of unsupervised machine learning. We can ask whether the clustering provided is a 'good' one using the measurement of a quantity called the *silhouette*. This is defined in R documentation as follows:

For each observation i , the `_silhouette width_` $s(i)$ is defined as follows:

Put $a(i)$ = average dissimilarity between i and all other points of the cluster to which i belongs (if i is the `_only_` observation in its cluster, $s(i) := 0$ without further calculations). For all `_other_` clusters C , put $d(i, C)$ = average dissimilarity of i to all observations of C . The smallest of these $d(i, C)$ is $b(i) := \min_C d(i, C)$, and can be seen as the dissimilarity between i and its

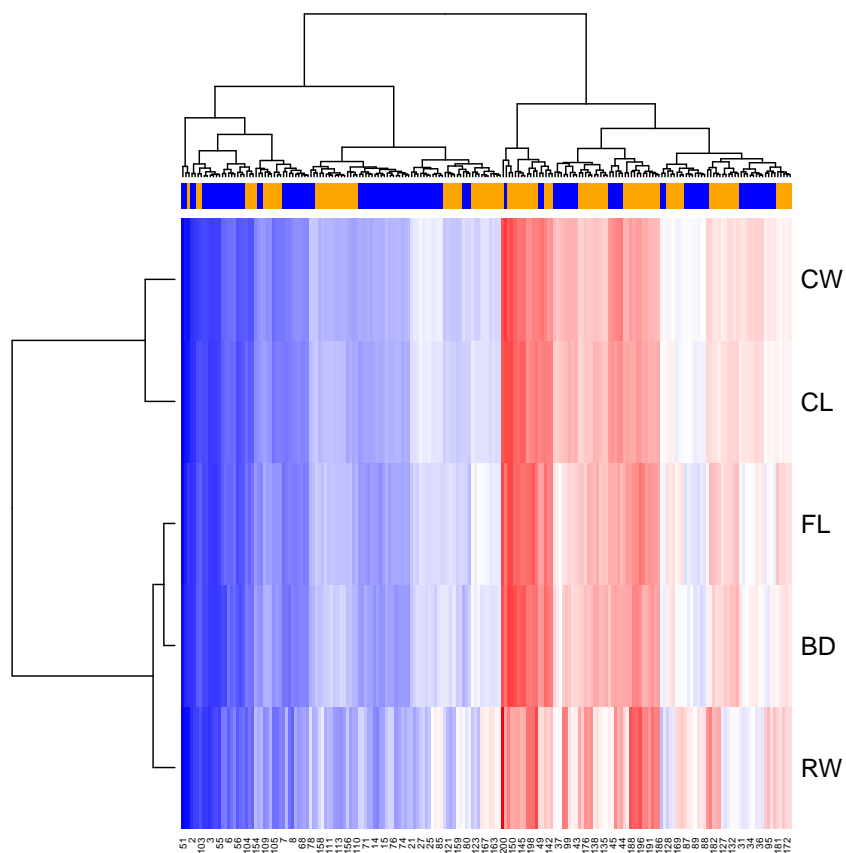


Figure 5: Heatmap plot of the `crabs` data, including dendrograms representing hierarchical clustering of the rows and columns.

"neighbor" cluster, i.e., the nearest one to which it does `_not_` belong. Finally,

$$s(i) := (b(i) - a(i)) / \max(a(i), b(i)).$$

We can compute the silhouette for any partition of a dataset, and can use the hierarchical clustering result to define a partition as follows:

```
> cl = hclust(dist(X))
> tr = cutree(cl,2)
> table(tr)
```

```
tr
  1  2
105 95

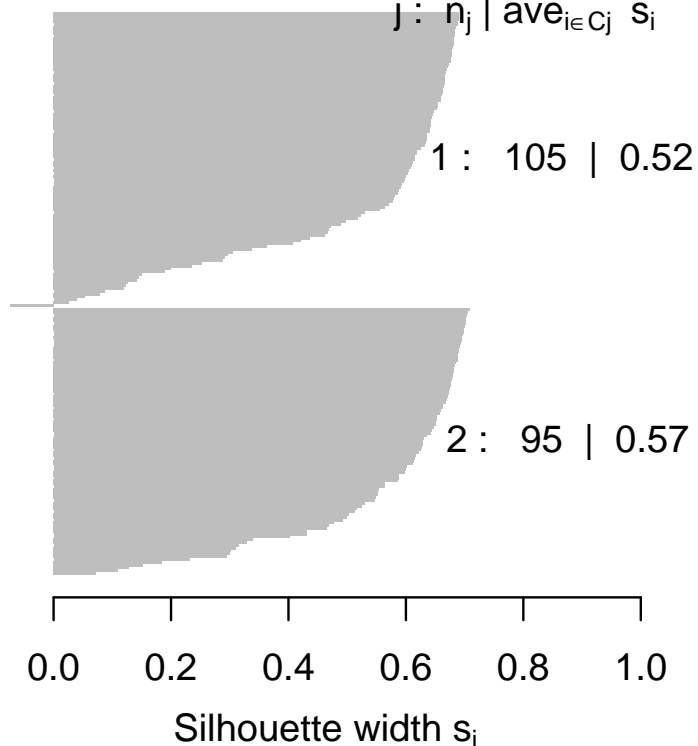
> library(cluster)
> sil = silhouette( tr, dist(X) )
> plot(sil)
```

Silhouette plot of (x = tr, dist = dist

n = 200

2 clusters C_j

$j : n_j \mid \text{ave}_{i \in C_j} s_i$



Average silhouette width : 0.55

- *Question 8.* In the preceding, we have used default `dist`, and default clustering algorithm for the heatmap. Investigate the impact of altering the choice of distance and clustering method on the clustering performance, both in relation to capacity to recover groups defined by species and in relation to the silhouette distribution.

- *Question 9.* The PCA shows that the data configuration in PC2 and PC3 is at least bifurcated. Apply hierarchical and K-means clustering to the two-dimensional data in this subspace, and compare results with respect to capturing the species \times gender labels, and with respect to silhouette values. For example, load the `exprs` slot of `crES` [see just below for the definition of this structure] with the PCA reexpression of the features, call the result `pcrES`, and then:

```
> ff = kmeansB(pcrES[2:3,], k=4)
> table(ff@clustIndices, crES$spsex)
```

2.6 Supervised learning

In this section we will examine procedures for polychotomous prediction. We want to be able to use the measurements to predict both species and sex of the crab. Again we would like to use the `MLInterfaces` infrastructure, so an `ExpressionSet` container will be useful.

```
> feat2 = t(data.matrix(crabs[, -c(1:3)]))
> pd2 = new("AnnotatedDataFrame", crabs[,1:2])
> crES = new("ExpressionSet", exprs=feat2, phenoData=pd2)
> crES$spsex = paste(crES$sp, crES$sex, sep=":")
> table(crES$spsex)
```

```
B:F B:M O:F O:M
50  50  50  50
```

We will permute the samples so that simple selections for training set indices are random samples.

```
> set.seed(1234)
> crES = crES[, sample(1:200, size=200, replace=FALSE)]
```

2.6.1 RPART

A classic procedure is recursive partitioning.

```
> library(rpart)
> tr1 = MLearn(spsex~., crES, rpartI, 1:140)
> tr1
```

`MLInterfaces` classification output container

The call was:

```
MLearn(formula = spsex ~ ., data = crES, .method = rpartI, trainInd = 1:140)
Predicted outcome distribution for test set:
```

```

B:F B:M O:F O:M
 15 20 12 13
Summary of scores on test set (use testScores() method for details):
      B:F      B:M      O:F      O:M
0.1847013 0.3631000 0.2205201 0.2316786

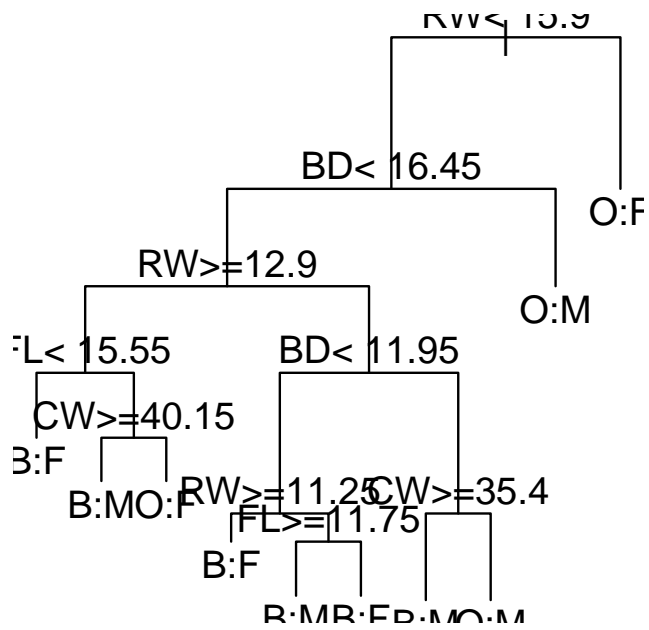
> confuMat(tr1)

      predicted
given B:F B:M O:F O:M
  B:F  11   2   5   0
  B:M   4  11   0   4
  O:F   0   3   7   3
  O:M   0   4   0   6

      The actual tree is

> plot(RObject(tr1))
> text(RObject(tr1))

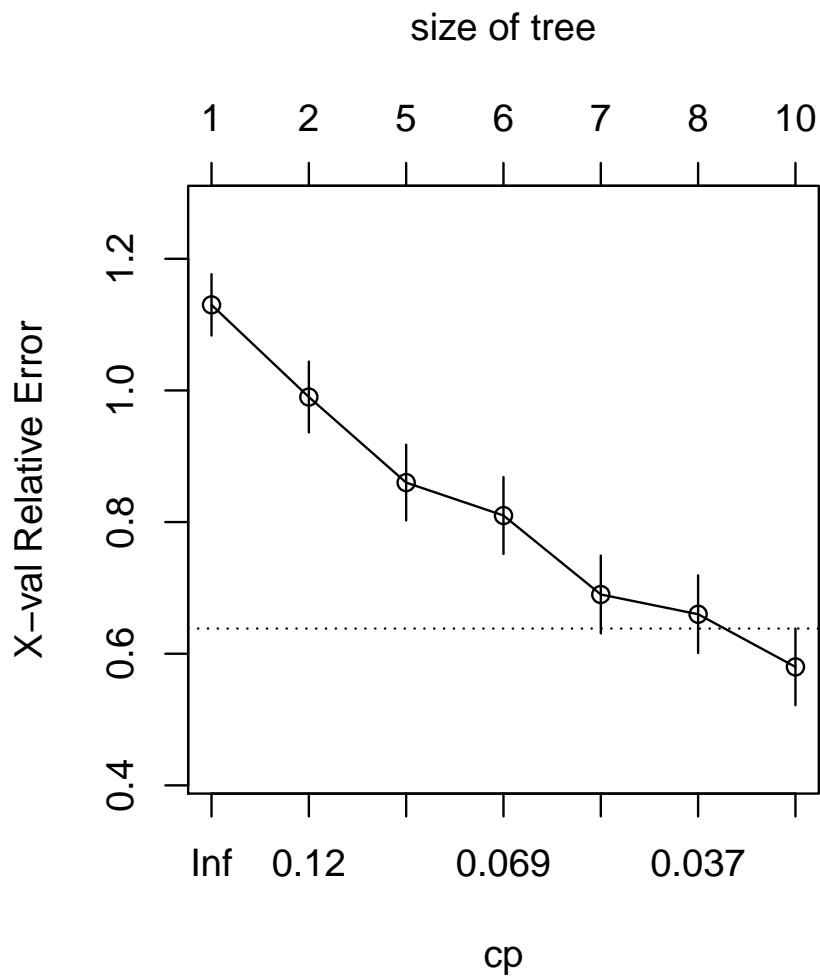
```



cludes a diagnostic tool called the cost-complexity plot:

```
> plotcp(RObject(tr1))
```

This procedure in-



2.6.2 Random forests

A generalization of recursive partitioning is obtained by creating a collection of trees by bootstrap-sampling cases and randomly sampling from features available for splitting at nodes.

```
> set.seed(124)
> library(randomForest)
> rf1 = MLearn(spsex~., crES, randomForestI, 1:140 )
> rf1
```

MLInterfaces classification output container

The call was:


```

MLearn(formula = spsex ~ ., data = crES, .method = randomForestI,
        trainInd = 1:140)
Predicted outcome distribution for test set:

B:F B:M O:F O:M
 14  21  12  13
Summary of scores on test set (use testScores() method for details):
      B:F      B:M      O:F      O:M
0.2479667 0.3208333 0.2184333 0.2127667

> cm = confuMat(rf1)
> cm

```

```

      predicted
given B:F B:M O:F O:M
  B:F  13   2   2   1
  B:M   1  14   1   3
  O:F   0   2   9   2
  O:M   0   3   0   7

```

The single split error rate is estimated at 28%.

- *Question 10.* What is the out-of-bag error rate for rf1? Obtain a cross-validated estimate of misclassification error using randomForest with an xvalSpec().

2.6.3 Linear discriminants

```

> ld1 = MLearn(spsex~., crES, ldaI, 1:140 )
> ld1

MLInterfaces classification output container
The call was:
MLearn(formula = spsex ~ ., data = crES, .method = ldaI, trainInd = 1:140)
Predicted outcome distribution for test set:

B:F B:M O:F O:M
 19  18  12  11

> confuMat(ld1)

      predicted
given B:F B:M O:F O:M

```

```

B:F  17   1   0   0
B:M   2  17   0   0
O:F   0   0  12   1
O:M   0   0   0  10

```

```

> xvld = MLearn( spsex~., crES, ldaI, xvalSpec("LOG", 5, balkfold.xvspec(5)))
> confuMat(xvld)

```

```

      predicted
given B:F B:M O:F O:M
B:F  49   1   0   0
B:M   5  45   0   0
O:F   0   0  46   4
O:M   0   0   0  50

```

- *Question 11.* Use the balkfold function to generate an index set for partitions that is balanced with respect to class distribution. Check the balance and repeat the cross validation.

2.6.4 Neural net

```

> nn1 = MLearn(spsex~., crES, nnetI, 1:140, size=3, decay=.1)

```

```

# weights:  34
initial  value 204.761335
iter  10 value 190.034085
iter  20 value 152.030689
iter  30 value 144.383484
iter  40 value 69.695971
iter  50 value 34.809031
iter  60 value 32.800275
iter  70 value 32.731441
iter  80 value 32.725763
iter  90 value 32.725726
iter  90 value 32.725726
iter  90 value 32.725726
final  value 32.725726
converged

```

```

> nn1

```

MLInterfaces classification output container
The call was:

```
MLearn(formula = spsex ~ ., data = crES, .method = nnetI, trainInd = 1:140,
        size = 3, decay = 0.1)
```

Predicted outcome distribution for test set:

```
B:F B:M O:F O:M
```

```
18 19 12 11
```

Summary of scores on test set (use testScores() method for details):

```
      B:F      B:M      O:F      O:M
0.2984750 0.3050544 0.2114445 0.1850261
```

```
> RObject(nn1)
```

a 5-3-4 network with 34 weights

inputs: FL RW CL CW BD

output(s): spsex

options were - softmax modelling decay=0.1

```
> confuMat(nn1)
```

```
      predicted
given B:F B:M O:F O:M
B:F  17   1   0   0
B:M   1  18   0   0
O:F   0   0  12   1
O:M   0   0   0  10
```

```
> xvnnBAD = MLearn( spsex~., crES, nnetI,
+   xvalSpec("LOG", 5, function(data, clab, iternum) {
+     which( rep(1:5,each=40) == iternum ) } ),
+   size=3, decay=.1 )
> xvnnGOOD = MLearn( spsex~., crES, nnetI,
+   xvalSpec("LOG", 5, balKfold.xvspec(5) ),
+   size=3, decay=.1 )
```

```
> confuMat(xvnnBAD)
```

```
      predicted
given B:F B:M O:F O:M
B:F  49   1   0   0
B:M   5  45   0   0
O:F   0   0  46   4
O:M   0   0   3  47
```

```
> confuMat(xvnnGOOD)
```

```

      predicted
given B:F B:M O:F O:M
  B:F  49   1   0   0
  B:M   4  46   0   0
  O:F   0   0  49   1
  O:M   0   0   0  50

```

2.6.5 SVM

```
> sv1 = MLearn(spsex~., crES, svmI, 1:140)
> sv1
```

MLInterfaces classification output container

The call was:

```
MLearn(formula = spsex ~ ., data = crES, .method = svmI, trainInd = 1:140)
Predicted outcome distribution for test set:
```

```

B:F B:M O:F O:M
 22 14 12 12

```

Summary of scores on test set (use testScores() method for details):

```

      B:M      B:F      O:M      O:F
0.2255516 0.2988727 0.2209848 0.2545908

```

```
> RObject(sv1)
```

Call:

```
svm(formula = formula, data = data, probability = probability)
```

Parameters:

```

  SVM-Type:  C-classification
  SVM-Kernel: radial
      cost:  1

```

Number of Support Vectors: 129

```
> confuMat(sv1)
```

```

      predicted
given B:F B:M O:F O:M

```

```

B:F  16   0   2   0
B:M   5  11   0   3
O:F   1   1  10   1
O:M   0   2   0   8

> xvsv = MLearn( spsex~., crES, svmI, xvalSpec("LOG", 5,
+       balkfold.xvspec(5)))

> confuMat(xvsv)

      predicted
given B:F B:M O:F O:M
B:F  45   0   5   0
B:M  12  35   0   3
O:F   9   0  40   1
O:M   4   0   0  46

```

3 Learning with expression arrays

Here we will concentrate on ALL: acute lymphocytic leukemia, B-cell type.

3.1 Phenotype reduction

We will identify expression patterns that discriminate individuals with BCR/ABL fusion in B-cell leukemia.

```

> library("ALL")
> data("ALL")
> bALL = ALL[, substr(ALL$BT,1,1) == "B"]
> fus = bALL[, bALL$mol.biol %in% c("BCR/ABL", "NEG")]
> fus$mol.biol = factor(fus$mol.biol)
> fus

```

```

ExpressionSet (storageMode: lockedEnvironment)
assayData: 12625 features, 79 samples
  element names: exprs
protocolData: none
phenoData
  sampleNames: 01005 01010 ... 84004 (79 total)
  varLabels: cod diagnosis ... date last seen (21 total)
  varMetadata: labelDescription
featureData: none

```

```
experimentData: use 'experimentData(object)'  
  pubMedIds: 14684422 16243790  
Annotation: hgu95av2
```

3.2 Nonspecific filtering

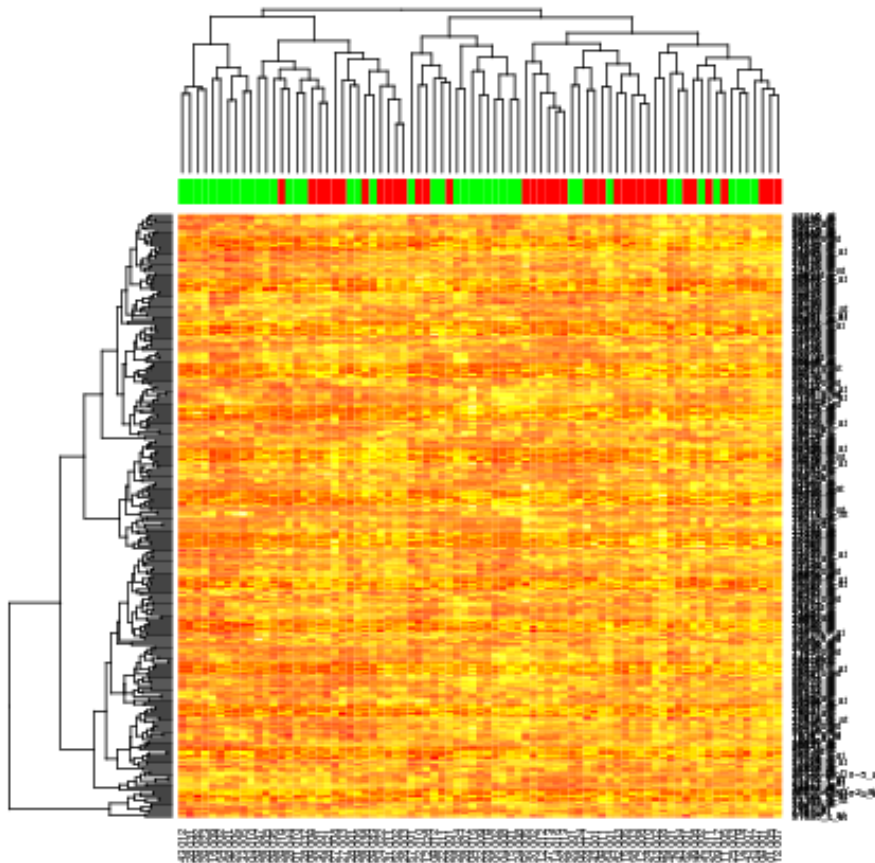
We can nonspecifically filter to 300 genes (to save computing time) with largest measures of robust variation across all samples:

```
> mads = apply(exprs(fus),1,mad)  
> fusk = fus[ mads > sort(mads,decr=TRUE)[300], ]  
> fcol = ifelse(fusk$mol.biol=="NEG", "green", "red")
```

3.3 Exploratory work

For exploratory data analysis, a heatmap is customary.

```
> heatmap(exprs(fusk), ColSideColors=fcol)
```

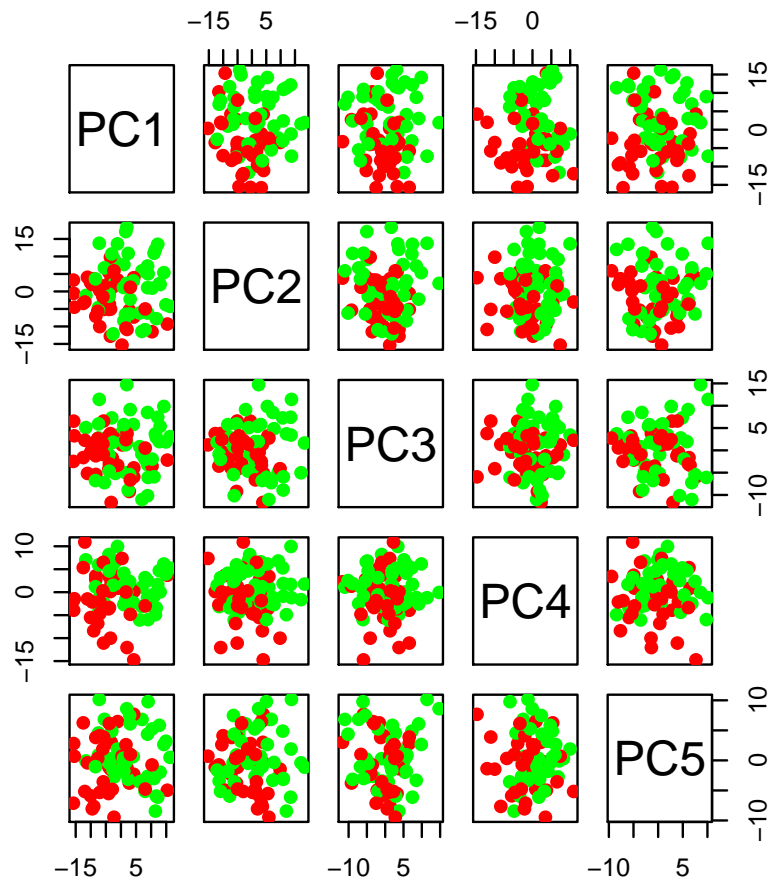


Principal components and a biplot may be more revealing. How many principal components are likely to be important?

```
> PCg = prcomp(t(exprs(fusk)))
> plot(PCg)
```



```
> pairs(PCg$x[,1:5],col=fcol,pch=19)
```

```
> biplot(PCg)
```


3.4 Classifier construction

3.4.1 Demonstrations

Diagonal LDA has a good reputation. Let's try it first, followed by neural net and random forests. We will not attend to tuning the latter two, defaults or guesses for key parameters are used.

```
> dld1 = MLearn( mol.biol~., fusk, dldaI, 1:40 )
```

```
> dld1
```

MLInterfaces classification output container

The call was:

```
MLearn(formula = mol.biol ~ ., data = fusk, .method = dldaI,  
       trainInd = 1:40)
```

Predicted outcome distribution for test set:

BCR/ABL	NEG
27	12

```
> confuMat(dld1)
```

	predicted	
given	BCR/ABL	NEG
BCR/ABL	15	1
NEG	12	11

```
> nnALL = MLearn( mol.biol~., fusk, nnetI, 1:40, size=5, decay=.01,  
+   MaxNWts=2000 )
```

```
# weights: 1506  
initial value 30.461691  
iter 10 value 12.986715  
iter 20 value 7.220767  
iter 30 value 4.938725  
iter 40 value 3.700680  
iter 50 value 1.648254  
iter 60 value 1.557908  
iter 70 value 0.995742  
iter 80 value 0.772829  
iter 90 value 0.681422  
iter 100 value 0.649037  
final value 0.649037  
stopped after 100 iterations
```

```
> confuMat(nnALL)
```

	predicted	
given	BCR/ABL	NEG
BCR/ABL	15	1
NEG	8	15

```
> rfALL = MLearn( mol.biol~., fusk, randomForestI, 1:40 )
```

```
> rfALL
```

MLInterfaces classification output container

The call was:

```
MLearn(formula = mol.biol ~ ., data = fusk, .method = randomForestI,
        trainInd = 1:40)
```

Predicted outcome distribution for test set:

BCR/ABL	NEG
24	15

Summary of scores on test set (use testScores() method for details):

BCR/ABL	NEG
0.5284615	0.4715385

```
> confuMat(rfALL)
```

	predicted	
given	BCR/ABL	NEG
BCR/ABL	15	1
NEG	9	14

None of these are extremely impressive, but the problem may just be very hard. An interesting proposal is RDA, regularized discriminant analysis (package *rda*, Guo, Hastie, Tibshirani 2007 Biostatistics). This algorithm recognizes the fact that covariance matrix estimation in high dimensional data is very inaccurate, so the estimator is shrunk towards the identity. We have a rudimentary interface, in which the key parameters are chosen by native cross-validation (in *rda.cv*) and then applied once to get the final object.

```
> set.seed(1234)
```

```
> rdaALL = MLearn( mol.biol~., fusk, rdacvI, 1:40 )
```

```
> rdaALL
```

MLInterfaces classification output container

The call was:

```
MLearn(formula = mol.biol ~ ., data = fusk, .method = rdacvI,  
        trainInd = 1:40)
```

Predicted outcome distribution for test set:

BCR/ABL	NEG
21	18

```
> confuMat(rdaALL)
```

	predicted	
given	BCR/ABL	NEG
BCR/ABL	15	1
NEG	6	17

A by-product of the algorithm is a set of retained genes that were found to play a role in discrimination. This can be established as follows:

```
> library(hgu95av2.db)  
> psid = RObject(rdaALL)$keptFeatures  
> psid = gsub("^X", "", psid) # make.names is run inopportunately  
> mget(psid, hgu95av2GENENAME, ifnotfound=NA)[1:5]
```

```
$`1113_at`
```

```
[1] "bone morphogenetic protein 2"
```

```
$`1178_at`
```

```
[1] "dihydrofolate reductase"
```

```
$`1520_s_at`
```

```
[1] "interleukin 1 beta"
```

```
$`1635_at`
```

```
[1] "ABL proto-oncogene 1, non-receptor tyrosine kinase"
```

```
$`1674_at`
```

```
[1] "YES proto-oncogene 1, Src family tyrosine kinase"
```

- *Question 14.* How can we assess the relative impacts of regularization (expanding the covariance model beyond that of DLDA, which was shown above to do poorly, but without relying on the full covariance) and implicit feature selection conducted in RDA?

3.4.2 Gene set appraisal

- *Question 15.* We can assess the predictive capacity of a set of genes by restricting the ExpressionSet to that set and using the best classifier appropriate to the problem. We can also assess the incremental effect of combining gene sets, relative to using them separately.

One collection of gene sets that is straightforward to use and interpret is provided by the keggorthology package (see also GSEABase). Here's how we can define the ExpressionSets for genes annotated by KEGG to Environmental (Genetic) Information Processing:

```
> library(keggorthology)
> data(KOgraph)
> adj(KOgraph, nodes(KOgraph)[1])

$KO.Feb10root
[1] "Metabolism"
[2] "Genetic Information Processing"
[3] "Environmental Information Processing"
[4] "Cellular Processes"
[5] "Organismal Systems"
[6] "Human Diseases"

> EIP = getKOprobes("Environmental Information Processing")
> GIP = getKOprobes("Genetic Information Processing")
> length(intersect(EIP, GIP))

[1] 40

> EIPi = setdiff(EIP, GIP)
> GIP = setdiff(GIP, EIP)
> EIP = EIPi
> Efusk = fusk[ featureNames(fusk) %in% EIP, ]
> Gfusk = fusk[ featureNames(fusk) %in% GIP, ]
```

Obtain and assess the predictive capacity of the genes annotated to "Cell Growth and Death".

- *Question 16.* How many of the genes identified by RDA as important for discriminating fusion are annotated to Genetic Information Processing in the KEGG orthology?

4 Embedding features selection in cross-validation

We provide helper functions to conduct several kinds of feature selection in cross-validation, see `help(fs.absT)`. Here we pick the top 30 features (ranked by absolute t statistic) for each cross-validation partition.

```
> dldFS = MLearn( mol.biol~., fusk, dldaI, xvalSpec("LOG", 5,
+   balkfold.xvspec(5), fs.absT(30) ))
> dldFS
```

MLInterfaces classification output container

The call was:

```
MLearn(formula = mol.biol ~ ., data = fusk, .method = dldaI,
      trainInd = xvalSpec("LOG", 5, balkfold.xvspec(5), fs.absT(30)))
```

Predicted outcome distribution for test set:

BCR/ABL	NEG
42	37

history of feature selection in cross-validation available; use `fsHistory()`

```
> confuMat(dld1)
```

	predicted	
given	BCR/ABL	NEG
BCR/ABL	15	1
NEG	12	11

```
> confuMat(dldFS)
```

	predicted	
given	BCR/ABL	NEG
BCR/ABL	34	3
NEG	8	34

5 Session information

```
> sessionInfo()
```

```
R version 3.6.1 (2019-07-05)
```

```
Platform: x86_64-apple-darwin15.6.0 (64-bit)
```

```
Running under: OS X El Capitan 10.11.6
```

```
Matrix products: default
```

```
BLAS: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRblas.0.dylib
```

```
LAPACK: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRlapack.dylib
```

```
locale:
```

```
[1] C/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
```

```
attached base packages:
```

```
[1] stats4      parallel  stats      graphics  grDevices  utils      datasets
```

```
[8] methods     base
```

```
other attached packages:
```

```
[1] keggorthology_2.36.0 graph_1.62.0          hgu95av2.db_3.2.3
[4] org.Hs.eg.db_3.8.2   ALL_1.26.0           randomForest_4.6-14
[7] rpart_4.1-15         lattice_0.20-38      MASS_7.3-51.4
[10] golubEsets_1.26.0    MLInterfaces_1.64.1  cluster_2.1.0
[13] annotate_1.62.0       XML_3.98-1.20        AnnotationDbi_1.46.1
[16] IRanges_2.18.3       S4Vectors_0.22.1     Biobase_2.44.0
[19] BiocGenerics_0.30.0
```

```
loaded via a namespace (and not attached):
```

```
[1] sfsmisc_1.1-4        bit64_0.9-7          splines_3.6.1        gtools_3.8.1
[5] threejs_0.3.1        shiny_1.4.0          assertthat_0.2.1     blob_1.2.0
[9] robustbase_0.93-5    pillar_1.4.2         RSQLite_2.1.2        backports_1.1.5
[13] glue_1.3.1           digest_0.6.21        RColorBrewer_1.1-2   promises_1.1.0
[17] gbm_2.1.5            htmltools_0.4.0      httpuv_1.5.2         Matrix_1.2-17
[21] rda_1.0.2-2.1        mlbench_2.1-1        pkgconfig_2.0.3      genefilter_1.66.0
[25] purrr_0.3.2          xtable_1.8-4         gdata_2.18.0         later_1.0.0
[29] tibble_2.1.3         ggvis_0.4.4          nnet_7.3-12          ada_2.0-5
[33] survival_2.44-1.1    magrittr_1.5         crayon_1.3.4         mime_0.7
[37] mclust_5.4.5         memoise_1.1.0        hwriter_1.3.2        class_7.3-15
[41] tools_3.6.1          kernlab_0.9-27       fpc_2.2-3            e1071_1.7-2
[45] pls_2.7-2            compiler_3.6.1       rlang_0.4.0          grid_3.6.1
```


[49]	RCurl_1.95-4.12	htmlwidgets_1.5.1	crosstalk_1.0.0	igraph_1.2.4.1
[53]	bitops_1.0-6	base64enc_0.1-3	gtable_0.3.0	flexmix_2.3-15
[57]	DBI_1.0.0	R6_2.4.0	gridExtra_2.3	prabclus_2.3-1
[61]	dplyr_0.8.3	fastmap_1.0.1	bit_1.1-14	zeallot_0.1.0
[65]	modeltools_0.2-22	Rcpp_1.0.2	vctrs_0.2.0	DEoptimR_1.0-8
[69]	tidyselect_0.2.5	diptest_0.75-7		