

# Differential analyses with DSS

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### Abstract

This vignette introduces the use of the Bioconductor package DSS (Dispersion Shrinkage for Sequencing data), which is designed for differential analysis based on high-throughput sequencing data. It performs differential expression analyses for RNA-seq, and differential

methylation analyses for bisulfite sequencing (BS-seq) data. The core of DSS is a procedure based on Bayesian hierarchical model to estimate and shrink gene- or CpG site-specific dispersions, then conduct Wald tests for detecting differential expression/methylation.

# 1 Introduction

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Recent advances in various high-throughput sequencing technologies have revolutionized genomics research. Among them, RNA-seq is designed to measure the abundance of RNA products, and Bisulfite sequencing (BS-seq) is for measuring DNA methylation. A fundamental question in functional genomics research is whether gene expression or DNA methylation vary under different biological contexts. Thus, identifying differential expression genes (DEGs) or differential methylation loci/regions (DML/DMRs) are key tasks in RNA-seq or BS-seq data analyses.

The differential expression (DE) or differential methylation (DM) analyses are often based on gene- or CpG-specific statistical test. A key limitation in RNA- or BS-seq experiments is that the number of biological replicates is usually limited due to cost constraints. This can lead to unstable estimation of within group variance, and subsequently undesirable results from hypothesis testing. Variance shrinkage methods have been widely applied in DE analyses in microarray data to improve the estimation of gene-specific within group variances. These methods are typically based on a Bayesian hierarchical model, with a prior imposed on the gene-specific variances to provide a basis for information sharing across all genes.

A distinct feature of RNA-seq or BS-seq data is that the measurements are in the form of counts and have to be modeled by discrete distributions. Unlike continuous distributions (such as Gaussian), the variances depend on means in these discrete distributions. This implies that the sample variances do not account for biological variation, and shrinkage cannot be applied on variances directly. In DSS, we assume that the count data are from the Gamma-Poisson (for RNA-seq) or Beta-Binomial (for BS-seq) distribution. We then parameterize the distributions by a mean and a dispersion parameters. The dispersion parameters, which represent the biological variation for replicates within a treatment group, play a central role in the differential analyses.

DSS implements a series of DE/DM detection algorithms based on the dispersion shrinkage method followed by Wald statistical test to test each gene/CpG site for differential expression/methylation. It provides functions for RNA-seq DE analysis for both two group comparison and multi-factor design, BS-seq DM analysis for two group comparison, multi-factor design, and data without biological replicate. Simulation and real data results show that the methods provides excellent performance compared to existing methods, especially when the overall dispersion level is high or the number of replicates is small.

For more details of the data model, the shrinkage method, and test procedures, please read [4] for differential expression from RNA-seq, [1] for differential methylation for two-group comparison from BS-seq, [2] for differential methylation for data without biological replicate, and [3] for differential methylation for general experimental design.

## 2 Using DSS for differential expression analysis

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### 2.1 Input data preparation

DSS requires a count table (a matrix of **integers**) for gene expression values (rows are for genes and columns are for samples). This is different from the isoform expression based analysis such as in cufflink/cuffdiff, where the gene expressions are represented as non-integers values. There are a number of ways to obtain the count table from raw sequencing data (fastq file), here we provide some example codes using several Bioconductor packages (the codes require installation of GenomicFeatures, Rsamtools, and GenomicRanges packages).

1. Sequence alignment. There are several RNA-seq aligner, for example, tophat or STAR. Assume the alignment result is saved in a BAM file `data.bam`.
2. Choose a gene annotation. GenomicFeatures package provides a convenient way to access different gene annotations. For example, if one wants to use RefSeq annotation for human genome build hg19, one can use following codes:

```
> library(GenomicFeatures)
> txdb = makeTranscriptDbFromUCSC(genom="hg19", tablename="refGene")
> genes = genes(txdb)
```

3. Obtain count table based on the alignment results and gene annotation. This can be done in several steps. First read in the BAM file using the Rsamtools package:

```
> bam=scanBam("data.bam")
```

Next, create GRanges object for the aligned sequence reads.

```
> IRange.reads=GRanges(seqnames=Rle(bam$rname), ranges=IRanges(bam$pos, width=bam$qwidth))
```

Finally, use the countOverlaps function in GenomicRanges function to obtain the read counts overlap each gene.

```
> counts = countOverlaps(genes, IRange.reads)
```

There are other ways to obtain the counts, for example, using QuasR or easyRNASeq Bioconductor package. Please refer to the package vignettes for more details.

## 2.2 Single factor experiment

In single factor RNA-seq experiment, DSS also requires a vector representing experimental designs. The length of the design vector must match the number of columns of the count table. Optionally, normalization factors or additional annotation for genes can be supplied.

The basic data container in the package is SeqCountSet class, which is directly inherited from ExpressionSet class defined in Biobase. An object of the class contains all necessary information for a DE analysis: gene expression values, experimental designs, and additional annotations.

A typical DE analysis contains the following simple steps.

1. Create a SeqCountSet object using newSeqCountSet.
2. Estimate normalization factor using estNormFactors.
3. Estimate and shrink gene-wise dispersion using estDispersion
4. Two-group comparison using waldTest.

The usage of DSS is demonstrated in the simple simulation below.

1. First load in the library, and make a SeqCountSet object from some counts for 2000 genes and 6 samples.

```
> library(DSS)
> counts1=matrix(rnbinom(300, mu=10, size=10), ncol=3)
> counts2=matrix(rnbinom(300, mu=50, size=10), ncol=3)
> X1=cbind(counts1, counts2) ## these are 100 DE genes
> X2=matrix(rnbinom(11400, mu=10, size=10), ncol=6)
> X=rbind(X1,X2)
> designs=c(0,0,0,1,1,1)
> seqData=newSeqCountSet(X, designs)
> seqData

SeqCountSet (storageMode: lockedEnvironment)
assayData: 2000 features, 6 samples
  element names: exprs
protocolData: none
phenoData
  sampleNames: 1 2 ... 6 (6 total)
```

## Differential analyses with DSS

```
varLabels: designs
varMetadata: labelDescription
featureData: none
experimentData: use 'experimentData(object)'
Annotation:
```

2. Estimate normalization factor.

```
> seqData=estNormFactors(seqData)
```

3. Estimate and shrink gene-wise dispersions

```
> seqData=estDispersion(seqData)
```

4. With the normalization factors and dispersions ready, the two-group comparison can be conducted via a Wald test:

```
> result=waldTest(seqData, 0, 1)
> head(result,5)
```

	geneIndex	muA	muB	lfc	difExpr	stats	pval
71	71	5.666667	73.66667	-2.487156	-68.00000	-5.880854	4.081544e-09
30	30	7.333333	67.66667	-2.163568	-60.33333	-5.638859	1.711803e-08
10	10	6.333333	61.00000	-2.197225	-54.66667	-5.618964	1.921053e-08
37	37	7.000000	60.33333	-2.093235	-53.33333	-5.512994	3.527804e-08
49	49	6.000000	54.33333	-2.132496	-48.33333	-5.489830	4.023219e-08

	local.fdr	fdr
71	4.157910e-05	4.157910e-05
30	7.175504e-05	6.033463e-05
10	7.538524e-05	6.033463e-05
37	9.973151e-05	6.922478e-05
49	1.060707e-04	7.992320e-05

A higher level wrapper function `DSS.DE` is provided for simple RNA-seq DE analysis in a two-group comparison. User only needs to provide a count matrix and a vector of 0's and 1's representing the design, and get DE test results in one line. A simple example is listed below:

```
> counts = matrix(rpois(600, 10), ncol=6)
> designs = c(0,0,0,1,1,1)
> result = DSS.DE(counts, designs)
> head(result)
```

	geneIndex	muA	muB	lfc	difExpr	stats	pval
88	88	13.62097	5.499697	0.8559521	8.121274	2.972550	0.002953372
84	84	11.28764	5.499697	0.6753424	5.787941	2.302844	0.021287628
71	71	10.90016	5.777374	0.5966755	5.122784	2.037815	0.041568477
51	51	10.36886	5.444040	0.6035126	4.924818	2.022702	0.043103864
81	81	12.67512	7.166364	0.5414877	5.508755	1.990121	0.046577557
17	17	13.95430	8.166364	0.5115430	5.787941	1.959784	0.050021077
	local.fdr	fdr					
88	0.4783396	0.4783396					
84	0.4432525	0.4205062					
71	0.6812562	0.4901884					
51	0.7018846	0.4901884					
81	0.7506451	0.5076290					
17	0.7990034	0.5076290					

## 2.3 Multifactor experiment

DSS provides functionalities for dispersion shrinkage for multifactor experimental designs. Downstream model fitting (through genealized linear model) and hypothesis testing can be performed using other packages such as edgeR, with the dispersions estimated from DSS.

Below is an example, based a simple simulation, to illustrate the DE analysis of a crossed design.

1. First simulate data for a 2x2 crossed experiments. Note the counts are randomly generated.

```
> library(DSS)
> library(edgeR)
> counts=matrix(rpois(800, 10), ncol=8)
> design=data.frame(gender=c(rep("M",4), rep("F",4)), strain=rep(c("WT", "Mutant"),4))
> X=model.matrix(~gender+strain, data=design)
```

2. make SeqCountSet, then estimate size factors and dispersion

```
> seqData=newSeqCountSet(counts, as.data.frame(X))
> seqData=estNormFactors(seqData)
> seqData=estDispersion(seqData)
```

3. Using edgeR's function to do glm model fitting, but plugging in the estimated dispersion from DSS.

```
> fit.edgeR <- glmFit(counts, X, dispersion=dispersion(seqData))
```

4. Using edgeR's function to do hypothesis testing on the second parameter of the model (gender).

```
> lrt.edgeR <- glmLRT(glmfit=fit.edgeR, coef=2)
> head(lrt.edgeR$table)
```

	logFC	logCPM	LR	PValue
1	-0.1430560	13.56519	0.1568407	0.6920820
2	0.2176198	13.40557	0.3103312	0.5774770
3	-0.1495152	13.59094	0.1777011	0.6733564
4	0.3087652	13.41017	0.6273497	0.4283291
5	0.2587115	13.64974	0.5458573	0.4600154
6	0.4664760	13.58976	1.6202821	0.2030525

## 3 Using DSS for differential methylation analysis

### 3.1 Overview

To detect differential methylation, statistical tests are conducted at each CpG site, and then the differential methylation loci (DML) or differential methylation regions (DMR) are called based on user specified threshold. A rigorous statistical tests should account for biological variations among replicates and the sequencing depth. Most existing methods for DM analysis are based on *ad hoc* methods. For example, using Fisher's exact ignores the biological variations, using t-test on estimated methylation levels ignores the sequencing depth. Sometimes arbitrary filtering are implemented: loci with depth lower than an arbitrary threshold are filtered out, which results in information loss

The DM detection procedure implemented in DSS is based on a rigorous Wald test for beta-binomial distributions. The test statistics depend on the biological variations (characterized by dispersion parameter) as well as the sequencing depth. An important part of the algorithm is the estimation of dispersion parameter, which is achieved through a shrinkage estimator based on a Bayesian hierarchical model [1]. An advantage of DSS is that the test can be performed even when there is no biological replicates. That's because by smoothing, the neighboring CpG sites can be viewed as "pseudo-replicates", and the dispersion can still be estimated with reasonable precision.

DSS also works for general experimental design, based on a beta-binomial regression model with “arcsine” link function. Model fitting is performed on transformed data with generalized least square method, which achieves much improved computational performance compared with methods based on generalized linear model.

DSS depends on `bsseq` Bioconductor package, which has neat definition of data structures and many useful utility functions. In order to use the DM detection functionalities, `bsseq` needs to be pre-installed.

### 3.2 Input data preparation

DSS requires data from each BS-seq experiment to be summarized into following information for each CG position: chromosome number, genomic coordinate, total number of reads, and number of reads showing methylation. For a sample, this information are saved in a simple text file, with each row representing a CpG site. Below shows an example of a small part of such a file:

chr	pos	N	X
chr18	3014904	26	2
chr18	3031032	33	12
chr18	3031044	33	13
chr18	3031065	48	24

One can follow below steps to obtain such data from raw sequence file (fastq file), using `bismark` (version 0.10.0, commands for newer versions could be different) for BS-seq alignment and count extraction. These steps require installation of `bowtie` or `bowtie2`, `bismark`, and the fasta file for reference genome.

1. Prepare Bisulfite reference genome. This can be done using the `bismark_genome_preparation` function (details in `bismark` manual). Example command is:  
`bismark_genome_preparation -path_to_bowtie /usr/local/bowtie/ -verbose /path/to/refgenomes/`
2. BS-seq alignment. Example command is:  
`bismark -q -n 1 -l 50 -path_to_bowtie /path/bowtie/ BS-refGenome reads.fastq`  
This step will produce two text files `reads.fastq_bismark.sam` and `reads.fastq_bismark_SE_report.txt`.
3. Extract methylation counts using `bismark_methylation_extractor` function:  
`bismark_methylation_extractor -s -bedGraph reads.fastq_bismark.sam`. This will create multiple txt files to summarize methylation call and cytosine context, a `bedGraph` file to display methylation percentage, and a coverage file containing counts information. The count file contain following columns: `chr`, `start`, `end`, `methylation%`, `count methylated`, `count unmethylated`. This file can be modified to make the input file for DSS.

A typical DML detection contains two simple steps. First one conduct DM test at each CpG site, then DML/DMR are called based on the test result and user specified threshold.

### 3.3 DML/DMR detection from two-group comparison

Below are the steps to call DML or DMR for BS-seq data in two-group comparison setting.

1. Load in library. Read in text files and create an object of BSseq class, which is defined in bsseq Bioconductor package. This step requires bsseq Bioconductor package. BSseq class is defined in that package.

```
> library(DSS)
> require(bsseq)
> path <- file.path(system.file(package="DSS"), "extdata")
> dat1.1 <- read.table(file.path(path, "cond1_1.txt"), header=TRUE)
> dat1.2 <- read.table(file.path(path, "cond1_2.txt"), header=TRUE)
> dat2.1 <- read.table(file.path(path, "cond2_1.txt"), header=TRUE)
> dat2.2 <- read.table(file.path(path, "cond2_2.txt"), header=TRUE)
> BSobj <- makeBSseqData( list(dat1.1, dat1.2, dat2.1, dat2.2),
+       c("C1", "C2", "N1", "N2") )[1:1000,]
> BSobj
```

```
An object of type 'BSseq' with
  1000 methylation loci
  4 samples
has not been smoothed
All assays are in-memory
```

2. Perform statistical test for DML by calling DMLtest function. This function basically performs following steps: (1) estimate mean methylation levels for all CpG site; (2) estimate dispersions at each CpG sites; (3) conduct Wald test. For the first step, there's an option for smoothing or not. Because the methylation levels show strong spatial correlations, smoothing can help obtain better estimates of mean methylation when the CpG sites are dense in the data (such as from the whole-genome BS-seq). However for data with sparse CpG, such as from RRBS or hydroxyl-methylation, smoothing is not recommended.

To perform DML test without smoothing, do:

```
> dmlTest <- DMLtest(BSobj, group1=c("C1", "C2"), group2=c("N1", "N2"))
Estimating dispersion for each CpG site, this will take a while ...
```

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```
> head(dmlTest)
```

	chr	pos	mu1	mu2	diff	diff.se	stat
1	chr18	3014904	0.3817233	0.4624549	-0.08073162	0.24997034	-0.3229648
2	chr18	3031032	0.3380579	0.1417008	0.19635711	0.11086362	1.7711592
3	chr18	3031044	0.3432172	0.3298853	0.01333190	0.12203116	0.1092500
4	chr18	3031065	0.4369377	0.3649218	0.07201587	0.10099395	0.7130711
5	chr18	3031069	0.2933572	0.5387464	-0.24538920	0.13178800	-1.8619996
6	chr18	3031082	0.3526311	0.3905718	-0.03794068	0.07847999	-0.4834440

	phi1	phi2	pval	fdr
1	0.300542998	0.01706260	0.74672190	0.9985094
2	0.008911745	0.04783892	0.07653423	0.6792127
3	0.010409029	0.01994821	0.91300423	0.9985094
4	0.010320888	0.01603200	0.47580174	0.9985094
5	0.012537553	0.02320887	0.06260315	0.6158797
6	0.007665696	0.01145531	0.62878051	0.9985094

To perform statistical test for DML with smoothing, do:

```
> dmlTest.sm <- DMLtest(BSobj, group1=c("C1", "C2"), group2=c("N1", "N2"), smoothing=TRUE)
```

Smoothing ...  
Estimating dispersion for each CpG site, this will take a while ...

User has the option to smooth the methylation levels or not. For WGBS data, smoothing is recommended so that information from nearby CpG sites can be combined to improve the estimation of methylation levels. A simple moving average algorithm is implemented for smoothing. In RRBS since the CpG coverage is sparse, smoothing might not alter the results much. If smoothing is requested, smoothing span is an important parameter which has non-trivial impact on DMR calling. We use 500 bp as default, and think that it performs well in real data tests.

3. With the test results, one can call DML by using `callDML` function. The results DMLs are sorted by the significance.

```
> dmls <- callDML(dmlTest, p.threshold=0.001)
```

```
> head(dmls)
```

	chr	pos	mu1	mu2	diff	diff.se	stat
450	chr18	3976129	0.01027497	0.9390339	-0.9287590	0.06544340	-14.19179
451	chr18	3976138	0.01027497	0.9390339	-0.9287590	0.06544340	-14.19179
638	chr18	4431501	0.01331553	0.9430566	-0.9297411	0.09273779	-10.02548

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```

639 chr18 4431511 0.01327049 0.9430566 -0.9297862 0.09270080 -10.02997
710 chr18 4564237 0.91454619 0.0119300 0.9026162 0.05260037 17.15988
782 chr18 4657576 0.98257334 0.0678355 0.9147378 0.06815000 13.42242
      phi1      phi2      pval      fdr postprob.overThreshold
450 0.052591567 0.02428826 1.029974e-45 2.499403e-43 1
451 0.052591567 0.02428826 1.029974e-45 2.499403e-43 1
638 0.053172411 0.07746835 1.177826e-23 1.429096e-21 1
639 0.053121697 0.07746835 1.125518e-23 1.429096e-21 1
710 0.009528898 0.04942849 5.302004e-66 3.859859e-63 1
782 0.010424723 0.06755651 4.468885e-41 8.133371e-39 1

```

By default, the test is based on the null hypothesis that the difference in methylation levels is 0. Alternatively, users can specify a threshold for difference. For example, to detect loci with difference greater than 0.1, do:

```

> dmls2 <- callDML(dmlTest, delta=0.1, p.threshold=0.001)
> head(dmls2)
      chr      pos      mu1      mu2      diff      diff.se      stat
450 chr18 3976129 0.01027497 0.9390339 -0.9287590 0.06544340 -14.19179
451 chr18 3976138 0.01027497 0.9390339 -0.9287590 0.06544340 -14.19179
638 chr18 4431501 0.01331553 0.9430566 -0.9297411 0.09273779 -10.02548
639 chr18 4431511 0.01327049 0.9430566 -0.9297862 0.09270080 -10.02997
710 chr18 4564237 0.91454619 0.0119300 0.9026162 0.05260037 17.15988
782 chr18 4657576 0.98257334 0.0678355 0.9147378 0.06815000 13.42242
      phi1      phi2      pval      fdr postprob.overThreshold
450 0.052591567 0.02428826 1.029974e-45 2.499403e-43 1
451 0.052591567 0.02428826 1.029974e-45 2.499403e-43 1
638 0.053172411 0.07746835 1.177826e-23 1.429096e-21 1
639 0.053121697 0.07746835 1.125518e-23 1.429096e-21 1
710 0.009528898 0.04942849 5.302004e-66 3.859859e-63 1
782 0.010424723 0.06755651 4.468885e-41 8.133371e-39 1

```

When delta is specified, the function will compute the posterior probability that the difference of the means is greater than delta. So technically speaking, the threshold for p-value here actually refers to the threshold for 1-posterior probability, or the local FDR. Here we use the same parameter name for the sake of the consistence of function syntax.

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4. DMR detection is also Based on the DML test results, by calling `callDMR` function. Regions with many statistically significant CpG sites are identified as DMRs. Some restrictions are provided by users, including the minimum length, minimum number of CpG sites, percentage of CpG site being significant in the region, etc. There are some *post hoc* procedures to merge nearby DMRs into longer ones.

```
> dmrs <- callDMR(dmlTest, p.threshold=0.01)
> head(dmrs)
```

	chr	start	end	length	nCG	meanMethy1	meanMethy2	diff.Methy	areaStat
27	chr18	4657576	4657639	64	4	0.506453	0.318348	0.188105	14.34236

Here the DMRs are sorted by "areaStat", which is defined in `bsseq` as the sum of the test statistics of all CpG sites within the DMR.

Similarly, users can specify a threshold for difference. For example, to detect regions with difference greater than 0.1, do:

```
> dmrs2 <- callDMR(dmlTest, delta=0.1, p.threshold=0.05)
> head(dmrs2)
```

	chr	start	end	length	nCG	meanMethy1	meanMethy2	diff.Methy	areaStat
31	chr18	4657576	4657639	64	4	0.5064530	0.3183480	0.188105	14.34236
19	chr18	4222533	4222608	76	4	0.7880276	0.3614195	0.426608	12.91667

Note that the distribution of test statistics (and p-values) depends on the differences in methylation levels and biological variations, as well as technical factors such as coverage depth. It is very difficult to select a natural and rigorous threshold for defining DMRs. We recommend users try different thresholds in order to obtain satisfactory results.

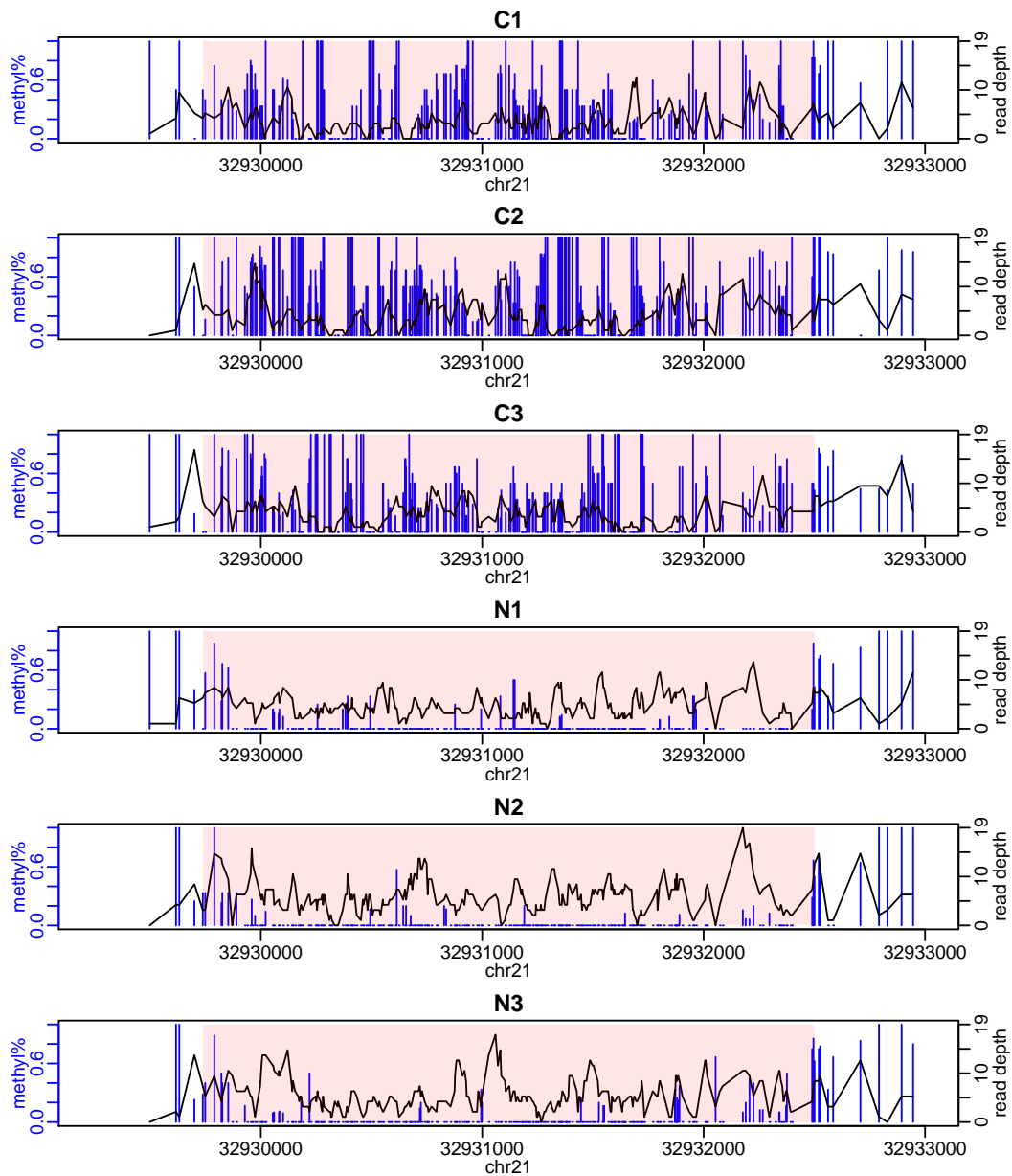
5. The DMRs can be visualized using `showOneDMR` function, This function provides more information than the `plotRegion` function in `bsseq`. It plots the methylation percentages as well as the coverage depths at each CpG sites, instead of just the smoothed curve. So the coverage depth information will be available in the figure.

To use the function, do

```
> showOneDMR(dmrs[1,], BSobj)
```

The result figure looks like the following. **Note that the figure below is not generated from the above example. The example data are from RRBS experiment so the DMRs are much shorter.**

Differential analyses with DSS



### 3.4 DML/DMR detection from general experimental design

In DSS, BS-seq data from a general experimental design (such as crossed experiment, or experiment with covariates) is modeled through a generalized linear model framework. We use “arcsine” link function instead of the typical logit link for it better deals with data at boundaries (methylation levels close to 0 or 1). Linear model fitting is done through ordinary least square on transformed methylation levels. Variance/covariance matrices for the estimates are derived with consideration of count data distribution and transformation.

#### 3.4.1 Hypothesis testing in general experimental design

In a general design, the data are modeled through a multiple regression thus there are multiple regression coefficients. In contrast, there is only one parameter in two-group comparison which is the difference between two groups. Under this type of design, hypothesis testing can be performed for one, multiple, or any linear combination of the parameters.

DSS provides flexible functionalities for hypothesis testing. User can test one parameter in the model through a Wald test, or any linear combination of the parameters through an F-test.

The `DMLtest.multiFactor` function provide interfaces for testing one parameter (through `coef` parameter), one term in the model (through `term` parameter), or linear combinations of the parameters (through `Contrast` parameter). We illustrate the usage of these parameters through a simple example below. Assume we have an experiment from three strains (A, B, C) and two sexes (M and F), each has 2 biological replicates (so there are 12 datasets in total).

```
> Strain = rep(c("A", "B", "C"), 4)
> Sex = rep(c("M", "F"), each=6)
> design = data.frame(Strain, Sex)
> design
```

	Strain	Sex
1	A	M
2	B	M
3	C	M
4	A	M
5	B	M
6	C	M
7	A	F
8	B	F

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9	C	F
10	A	F
11	B	F
12	C	F

To test the additive effect of Strain and Sex, a design formula is `Strain+Sex`, and the corresponding design matrix for the linear model is:

```
> X = model.matrix(~Strain+ Sex, design)
> X

      (Intercept) StrainB StrainC SexM
1             1      0      0      1
2             1      1      0      1
3             1      0      1      1
4             1      0      0      1
5             1      1      0      1
6             1      0      1      1
7             1      0      0      0
8             1      1      0      0
9             1      0      1      0
10            1      0      0      0
11            1      1      0      0
12            1      0      1      0
attr(,"assign")
[1] 0 1 1 2
attr(,"contrasts")
attr(,"contrasts")$Strain
[1] "contr.treatment"

attr(,"contrasts")$Sex
[1] "contr.treatment"
```

Under this design, we can do different tests using the `DMLtest.multiFactor` function:

- If we want to test the sex effect, we can either specify `coef=4`, `coef="SexM"`, or `term="Sex"`. Notice that when using character for `coef`, the character must match the column name of the design matrix, cannot do `coef="Sex"`. It is also important to note that using `term="Sex"` only tests a single parameter in the model because sex only has two levels.

## Differential analyses with DSS

- If we want to test the effect of Strain B versus Strain A (this is also testing a single parameter), we do `coef=2` or `coef="StrainB"`.
- If we want to test the whole Strain effect, it becomes a compound test because Strain has three levels. We do `term="Strain"`, which tests StrainB and StrainC simultaneously. We can also make a Contrast matrix L as following. It's clear that testing  $L^T\beta = 0$  is equivalent to testing StrainB=0 and StrainC=0.

```
> L = cbind(c(0,1,0,0),c(0,0,1,0))
> L

      [,1] [,2]
[1,]    0    0
[2,]    1    0
[3,]    0    1
[4,]    0    0
```

- One can perform more general test, for example, to test StrainB=StrainC, or that strains B and C has no difference (but they could be different from Strain A). In this case, we need to make following contrast matrix:

```
> matrix(c(0,1,-1,0), ncol=1)

      [,1]
[1,]    0
[2,]    1
[3,]   -1
[4,]    0
```

### 3.4.2 Example analysis for data from general experimental design

1. Load in data distributed with DSS. This is a small portion of a set of RRBS experiments. There are 5000 CpG sites and 16 samples. The experiment is a 2 design (2 cases and 2 cell types). There are 4 replicates in each case:cell combination.

```
> data(RRBS)
> RRBS

An object of type 'BSseq' with
  5000 methylation loci
  16 samples
has not been smoothed
All assays are in-memory
```

```
> design
      case cell
1      HC   rN
2      HC   rN
3      HC   rN
4      SLE  aN
5      SLE  rN
6      SLE  aN
7      SLE  rN
8      SLE  aN
9      SLE  rN
10     SLE  aN
11     SLE  rN
12     HC   aN
13     HC   aN
14     HC   aN
15     HC   aN
16     HC   rN
```

2. Fit a linear model using `DMLfit.multiFactor` function, include case, cell, and case:cell interaction.

```
> DMLfit = DMLfit.multiFactor(RRBS, design=design, formula=~case+cell+case:cell)

Fitting DML model for CpG site:
```

3. Use `DMLtest.multiFactor` function to test the cell effect. It is important to note that the `coef` parameter is the index of the coefficient to be tested for being 0. Because the model (as specified by formula in `DMLfit.multiFactor`) include intercept, the cell effect is the 3rd column in the design matrix, so we use `coef=3` here.

```
> DMLtest.cell = DMLtest.multiFactor(DMLfit, coef=3)
```

Alternatively, one can specify the name of the parameter to be tested. In this case, the input `coef` is a character, and it must match one of the column names in the design matrix. The column names of the design matrix can be viewed by

```
> colnames(DMLfit$X)
[1] "(Intercept)" "caseSLE" "cellrN" "caseSLE:cellrN"
```

## Differential analyses with DSS

The following line also works. Specifying `coef="cellrN"` is the same as specifying `coef=3`.

```
> DMLtest.cell = DMLtest.multiFactor(DMLfit, coef="cellrN")
```

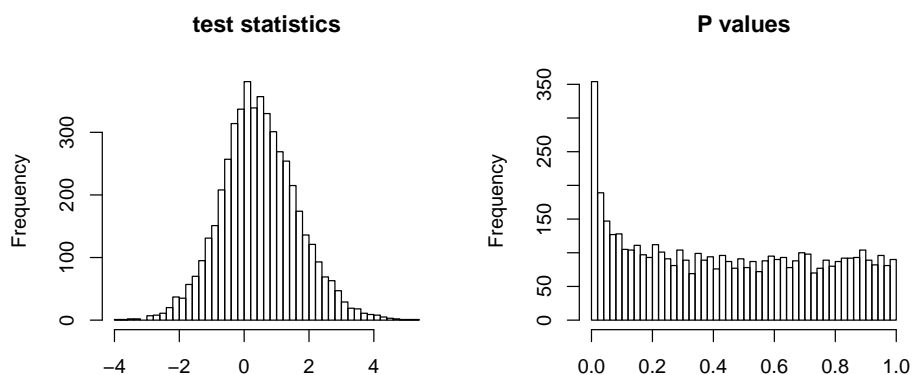
Result from this step is a data frame with chromosome number, CpG site position, test statistics, p-values (from normal distribution), and FDR. Rows are sorted by chromosome/position of the CpG sites. To obtain top ranked CpG sites, one can sort the data frame using following codes:

```
> ix=sort(DMLtest.cell[, "pvals"], index.return=TRUE)$ix
> head(DMLtest.cell[ix,])
```

	chr	pos	stat	pvals	fdrs
1273	chr1	2930315	5.280301	1.289720e-07	0.0006448599
4706	chr1	3321251	5.037839	4.708164e-07	0.0011770409
3276	chr1	3143987	4.910412	9.088510e-07	0.0015147517
2547	chr1	3069876	4.754812	1.986316e-06	0.0024828953
3061	chr1	3121473	4.675736	2.929010e-06	0.0029290097
527	chr1	2817715	4.441198	8.945925e-06	0.0065858325

Below is a figure showing the distributions of test statistics and p-values from this example dataset

```
> par(mfrow=c(1,2))
> hist(DMLtest.cell$stat, 50, main="test statistics", xlab="")
> hist(DMLtest.cell$pvals, 50, main="P values", xlab="")
```



4. DMRs for multifactor design can be called using `callDMR` function:

```
> callDMR(DMLtest.cell, p.threshold=0.05)

      chr  start    end length nCG  areaStat
33  chr1 2793724 2793907   184    5 12.619968
413 chr1 3309867 3310133   267    7 -12.093850
250 chr1 3094266 3094486   221    4 11.691413
262 chr1 3110129 3110394   266    5 11.682579
180 chr1 2999977 3000206   230    4 11.508302
121 chr1 2919111 2919273   163    4  9.421873
298 chr1 3146978 3147236   259    5  8.003469
248 chr1 3090627 3091585   959    5 -7.963547
346 chr1 3200758 3201006   249    4 -4.451691
213 chr1 3042371 3042459    89    5  4.115296
169 chr1 2995532 2996558  1027    4 -2.988665
```

Note that for results from for multifactor design, delta is NOT supported. This is because in multifactor design, the estimated coefficients in the regression are based on a GLM framework (loosely speaking), thus they don't have clear meaning of methylation level differences. So when the input DMLresult is from DMLtest.multiFactor, delta cannot be specified.

5. More flexible way to specify a hypothesis test. Following 4 tests should produce the same results, since 'case' only has two levels. However the p-values from F-tests (using term or Contrast) are slightly different, due to normal approximation in Wald test.

```
> ## fit a model with additive effect only
> DMLfit = DMLfit.multiFactor(RRBS, design, ~case+cell)

Fitting DML model for CpG site:

> ## test case effect
> test1 = DMLtest.multiFactor(DMLfit, coef=2)
> test2 = DMLtest.multiFactor(DMLfit, coef="caseSLE")
> test3 = DMLtest.multiFactor(DMLfit, term="case")
> Contrast = matrix(c(0,1,0), ncol=1)
> test4 = DMLtest.multiFactor(DMLfit, Contrast=Contrast)
> cor(cbind(test1$pval, test2$pval, test3$pval, test4$pval))

      [,1] [,2] [,3] [,4]
[1,]    1    1    1    1
[2,]    1    1    1    1
[3,]    1    1    1    1
[4,]    1    1    1    1
```

## Differential analyses with DSS

The model fitting and hypothesis test procedures are computationally very efficient. For a typical RRBS dataset with 4 million CpG sites, it usually takes less than half hour. In comparison, other similar software such as RADMeth or BiSeq takes at least 10 times longer.

## 4 Session Info

---

```
> sessionInfo()

R version 3.5.0 (2018-04-23)
Platform: x86_64-w64-mingw32/x64 (64-bit)
Running under: Windows Server 2012 R2 x64 (build 9600)

Matrix products: default

locale:
 [1] LC_COLLATE=C
 [2] LC_CTYPE=English_United States.1252
 [3] LC_MONETARY=English_United States.1252
 [4] LC_NUMERIC=C
 [5] LC_TIME=English_United States.1252

attached base packages:
 [1] splines      stats4      parallel      stats      graphics     grDevices     utils
 [8] datasets     methods     base

other attached packages:
 [1] edgeR_3.22.0           limma_3.36.0
 [3] DSS_2.28.0             bsseq_1.16.0
 [5] SummarizedExperiment_1.10.0 DelayedArray_0.6.0
 [7] BiocParallel_1.14.0     matrixStats_0.53.1
 [9] GenomicRanges_1.32.0    GenomeInfoDb_1.16.0
[11] IRanges_2.14.0          S4Vectors_0.18.0
[13] Biobase_2.40.0          BiocGenerics_0.26.0

loaded via a namespace (and not attached):
 [1] Rcpp_0.12.16           compiler_3.5.0         plyr_1.8.4
 [4] XVector_0.20.0         R.methodsS3_1.7.1      R.utils_2.6.0
 [7] bitops_1.0-6           tools_3.5.0            DelayedMatrixStats_1.2.0
[10] zlibbioc_1.26.0        digest_0.6.15          rhdf5_2.24.0
[13] evaluate_0.10.1        lattice_0.20-35        Matrix_1.2-14
[16] yaml_2.1.18            GenomeInfoDbData_1.1.0 stringr_1.3.0
[19] knitr_1.20             gtools_3.5.0           locfit_1.5-9.1
[22] rprojroot_1.3-2        grid_3.5.0             data.table_1.10.4-3
```

[25] HDF5Array_1.8.0	rmarkdown_1.9	Rhdf5lib_1.2.0
[28] magrittr_1.5	backports_1.1.2	scales_0.5.0
[31] htmltools_0.3.6	permute_0.9-4	BiocStyle_2.8.0
[34] colorspace_1.3-2	stringi_1.1.7	RCurl_1.95-4.10
[37] munsell_0.4.3	R.oo_1.22.0	

## References

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- [2] HAO WU, TIANLEI XU, HAO FENG, LI CHEN, BEN LI, BING YAO, ZHAOHUI QIN, PENG JIN AND KAREN N. CONNEELY. (2015). Detection of differentially methylated regions from whole-genome bisulfite sequencing data without replicates. *Nucleic Acids Research*. doi: 10.1093/nar/gkv715.
- [3] YONGSEOK PARK, HAO WU. (2016). Differential methylation analysis for BS-seq data under general experimental design. *Bioinformatics*. doi:10.1093/bioinformatics/btw026.
- [4] HAO WU, CHI WANG AND ZHIJING WU. (2013). A new shrinkage estimator for dispersion improves differential expression detection in RNA-seq data. *Biostatistics*. **14**(2), 232–243.