

Package ‘FRGEpistasis’

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Description A Tool for Epistasis Analysis Based on Functional Regression Model

License GPL-2

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FRGEpistasis-package *Package of Epistasis Detection by Functional Regression Model*

Description

FRGEpistasis is designed to detect the epistasis between genes or genomic regions for both common variants and rare variants. Currently FRGEpistasis was developed by Futao Zhang with R language and maintained in Xiong lab at UTSPH. This tool is friendly, convenient and memory efficient.

Details

Package: FRGEpistasis
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It currently has the following functional modules: Functional Regression Model (FRG) for Testing Interaction; Regression on Principal Components Analysis (PCA) for Testing Interaction; Point-wise interaction Test.

Author(s)

Futao Zhang Maintainer: Futao Zhang <futoaz@gmail.com>

fourierExpansion *Fourier Expansion of Genotype*

Description

This function aims to expand the genotype of one gene (or genomic region) with Fourier Expansion.

Usage

```
fourierExpansion(gene_idx, geno, gene_list, snp_map, rng)
```

Arguments

gene_idx	The expansion gene index in the gene annotation list.
geno	Genotype of all the genes in the gene annotation list.
gene_list	Gene annotation list which includes gene name, chromosome, start position and end position.
snp_map	SNP genetic map includes chromosome, snp identifier, genetic distance and base-pair position.
rng	A numeric value which represents gene region extensible scope.

Details

This function reduces the dimension of one gene(or genomic region) with Fourier Expansion. First extract out the genotype of this gene with the gene annotation and the SNP map information. Then expand the gene with the genotypes and SNP positions if the number of SNPs in the gene is over 3. Otherwise the raw genotypes of the gene would be returned. The number of Fourier Basis is selected to explain 80 percent of genetic variation.

Value

If the SNPs number of the gene is over 3, returns the expansion of the genotype which is a matrix with the dimension Sample number * Fourier Basis number. If the SNPs number of the gene is no more than 3, returns the raw genotype of the gene which is a matrix with the dimension Sample number * SNP number.

Author(s)

Futao Zhang

Examples

```
gLst<-read.csv(system.file("extdata", "gene.list.csv", package="fRGEpistasis"))
fdata<-read.table(system.file("extdata", "simGeno-chr1.raw", package="fRGEpistasis"),header=TRUE)
geno<-fdata[,-1:-6]
snp_map<-read.table(system.file("extdata", "chr1.map", package="fRGEpistasis"))
fourierExpansion(1, geno, gLst, snp_map, 0)
```

fRGEpistasis

Genome Wide Epistasis Study by Functional Regress Model

Description

This function is the entrance of the software package. It tests the Genome Wide Epistasis by Functional Regression Model.

Usage

```
fRGEpistasis(wDir, phenoInfo, gnoFiles, mapFiles, gLst, fdr, rng)
```

Arguments

wDir	The dataset directory. If the dataset is in the working directory, wDir is ".".
phenoInfo	It is a matrix with two columns. One column is the individual ID and the other is the phenotype. The phenotype can be quantitative trait or binary trait.
gnoFiles	The vector of genotype file names. It contains the genotype file names indicating where to read the genotype files.
mapFiles	The vector of SNP genetic map file names. It contains the map file names indicating where to read the genetic map files.
gLst	Gene annotation which includes gene name, chromosome, start position and end position.
fdr	FDR control threshold, When this value == 1, turn FDR control off.
rng	A numeric value which represents gene region extensible scope.

Details

Firstly this package reduces the dimension of genotype of all the genomic regions. Secondly this package tests the epistasis of genomic regions both of which are on the same chromosome(file). Thirdly this package tests the epistasis of genomic regions which are on different chromosomes(files).

This function is memory efficient with high performance. Memory efficiency: Only store reduced expansion data of genotypes instead of raw data of genotypes. This package reduces the dimension of genotype of all the genomic regions(see details of function "reduceGeno"). In real dataset the genotypes on different chromosome are always organized into different files. And each genotype file is very large. Reading all the files into memory is unacceptable. This package reads the files one by one and reduces the genotype dimension with Fourier expansion. In order to inform the package how many files and where to read, we need two data structures "gnoFiles" and "mapFiles" to store the file names.

high performance: Each data file only needs to read once and reduce dimension once. So I/O times are reduced and repeated computing of data reduction was avoided. This method is a kind of group test. We take a gene(or genomic region) as the test unit. The number of Test is sharply reduced comparing with point-wise interaction (SNP-SNP) test. The dimension of genotype is reduced by functional expansion, So the time of each test is reduced.

Value

Return a data frame which contains all the names of gene pairs and the p values of chi-square test for their epistasis.

Author(s)

Futao Zhang

Examples

```
wDir <-paste(system.file("extdata", package="FRGEpistasis"),"/",sep="")
gnoFiles<-read.table(system.file("extdata", "list_geno.txt", package="FRGEpistasis"))
mapFiles<-read.table(system.file("extdata", "list_map.txt", package="FRGEpistasis"))
phenoInfo <- read.csv(system.file("extdata", "phenotype.csv", package="FRGEpistasis"),header=TRUE)
gLst<-read.csv(system.file("extdata", "gene.list.csv", package="FRGEpistasis"))
rng=0
fdr=0.05
out_epi <- data.frame( )
```

```
phenoInfo [,2]=log(phenoInfo [,2])
out_epi = frgEpistasis(wDir,phenoInfo,gnoFiles,mapFiles,gLst,fdr,rng)
```

frgEpistasisTest *Epistasis Test by Functional Regression Model*

Description

This function is used to analyse the epistasis of genomic region A and genomic region B.

Usage

```
frgEpistasisTest(pheno, geno_A, pos_A, geno_B, pos_B)
```

Arguments

pheno	A vector of phenotype which can be quantitative trait or binary trait.
geno_A	Genotype matrix of gene (or genomic region) A.
pos_A	Vector of physical positions of SNPs in gene (or genomic region) A.
geno_B	Genotype matrix of gene (or genomic region) B.
pos_B	Vector of physical positions of SNPs in gene (or genomic region) B.

Details

This function is independent with other functions in this package. It is designed for small dataset test. It takes phenotype, genotype and Physical positions as the input. If the position information is NULL, this function considers the SNPs in this gene to be uniformly filled in the gene scope. First this function expands the genotypes of gene A and gene B. Then it analyses their epistasis.

Value

It returns the p value of chi-square test for epistasis detection between gene A and gene B.

Author(s)

Futao Zhang

Examples

```
smp_num=1000
number_snp_A=25
number_snp_B=20
pheno<-sample(c(0:500),smp_num,replace=TRUE)
smp1=rep(0,number_snp_A*smp_num)
idx_1=sample(c(1:(number_snp_A*smp_num)),ceiling(number_snp_A*smp_num/100))
idx_2=sample(c(1:(number_snp_A*smp_num)),ceiling(number_snp_A*smp_num/200))
smp1[idx_1]=1
smp1[idx_2]=2
geno_A=matrix(smp1,smp_num,number_snp_A)

smp1=sample(c(0,1,2),number_snp_B*smp_num,replace=TRUE)
geno_B=matrix(smp1,smp_num,number_snp_B)
```

```
fRGEpistasisTest(pheno, geno_A, pos_A=NULL, geno_B, pos_B=NULL)
```

fRGInteraction

Interaction Test by Functional Regression Model

Description

Test interaction between two gene (or genomic regions) with chi-squared test.

Usage

```
fRGInteraction(phenoData, x_A, x_B)
```

Arguments

phenoData	Vector of phenotype data which can be quantitative trait or binary trait.
x_A	Expansion data matrix of Genotype of gene A.
x_B	Expansion data matrix of Genotype of gene B.

Details

This function takes phenotype vector and expanded genotype matrices as input. It is the most important part of this software package. It is called by functions "innerEpi" and "innerEpi" of this package. The interaction between gene A and gene B is tested with chi-squared test.

Value

It returns the p value of chi-squared test for epistasis detection between gene A and gene B.

Author(s)

Futao Zhang

Examples

```
x_A<-as.matrix(rnorm(1000,mean=0,sd=1))
x_B<-as.matrix(rnorm(1000,mean=0,sd=1))
phenoData<-runif(1000,15,60)
fRGInteraction(phenoData,x_A,x_B)
```

`innerEpi`*Epistasis Detection Inner one Chromosome*

Description

Detect epistasis between 2 genes (or genomic regions) both of which are on the same chromosome.

Usage

```
innerEpi(pheno, gstnd, geno_expn, gname, gchr)
```

Arguments

<code>pheno</code>	Vector of phenotype data which can be quantitative trait or binary trait.
<code>gstnd</code>	Vector of indexes which indicates the start indexes and end indexes of expanded genotype of each gene on current chromosome in the matrix "geno_expn".
<code>geno_expn</code>	Matrix of expanded genotype data of all the genes.
<code>gname</code>	Vector of gene names on current chromosome.
<code>gchr</code>	Vector of Chromosome number of current chromosome.

Details

This function tests the epistasis between 2 genes both of which are on the same chromosome. It takes expanded genotype data as the input. First the data of the gene are extracted from "geno_expn" with "gstnd" and "gname". Then the function "FRGInteraction" will be called.

Value

Return a matrix which contains the gene names of the gene pairs and the p values of chi-squared test for the epistasis of the gene pairs.

Author(s)

Futao Zhang

Examples

```
smp_num<-1000
number_basis<-9
pheno<-sample(c(0:500),smp_num,replace=TRUE)
gname<-c("g1","g2")
gstnd<-c(0,5,9)
smp1<-runif(number_basis*smp_num, 0.0, 1.0)
geno_expn<-matrix(smp1,smp_num,number_basis)
gchr<-c(1,1)
innerEpi(pheno,gstnd,geno_expn,gname,gchr)
```

`innerSnplistInteraction`*Pairwise Interaction Test Inner The Same SNP List*

Description

Test the SNP-SNP interaction. And the SNPs are organized into one data structure.

Usage

```
innerSnplistInteraction(pheno, snpList)
```

Arguments

<code>pheno</code>	Vector of phenotype data.
<code>snpList</code>	Matrix of the genotypes of all the SNPs for testing the pairwise interactions.

Details

This function aims to test the pairwise interactions between the SNPs organized into the same data structure. It takes phenotype and genotypes of the SNPs as the input. And output all the p values for the interactions of SNP pairs.

Value

Return a frame contains names of all the SNPs pairs and p values for interactions of these pairs.

Author(s)

Futao Zhang

Examples

```
pheno<- round(runif(1000,40,60))
geno<- as.data.frame(matrix(round(runif(5000,0,2)),1000,5))
innerSnplistInteraction(pheno,geno)
```

`logTransPheno`*logarithmic transformation*

Description

Logarithmic Transformation of Phenotype

Usage

```
logTransPheno(pheno)
```


Arguments

pheno Vector of phenotype which is the quantitative trait.

Details

Some variables are not normally distributed. And using statistical tests on this data can give misleading results because they do not meet the statistical assumptions. Many variables have log-normal distributions.

Value

Return vector of transformed phenotype.

Examples

```
smp_num=100
pheno<-sample(c(0:500),smp_num,replace=TRUE)
logTransPheno(pheno)
```

 outerEpi

Epistasis Detection Outer Chromosomes

Description

Detect epistasis between 2 genes (or genomic regions) which are on different chromosomes.

Usage

```
outerEpi(pheno, gstnd, gStndp, geno_expn, gname, gNamep, gchr, gChrp)
```

Arguments

pheno Vector of phenotype data which can be quantitative trait or binary trait.

gstnd Vector of indexes which indicates the start indexes and end indexes of expanded genotype of each gene on one chromosome in the matrix "geno_expn".

gStndp Vector of indexes which indicates the start indexes and end indexes of expanded genotype of each gene on the other chromosome in the matrix "geno_expn".

geno_expn Matrix of expanded genotype data of all the genes.

gname Vector of gene names on one chromosome.

gNamep Vector of gene names on the other chromosome.

gchr Vector of Chromosome number of one chromosome.

gChrp Vector of Chromosome number of the other chromosome.

Details

This function tests the epistasis between 2 genes which are on different chromosomes. It takes expanded genotype data as the input. First the data of the gene are extracted from "geno_expn" with "gstnd" and "gname". Then the function "fRGInteraction" will be called.

Value

Return a matrix which contains the gene names of the gene pairs and the p values of chi-squared test for the epistasis of the gene pairs.

Author(s)

Futao Zhang

Examples

```
smp_num=1000
number_basis<-40
pheno<-sample(c(0:500), smp_num, replace=TRUE)
gname<-c("g1", "g2")
gNamep<-c("r1", "r2", "r3")
gstnd<-c(0, 5, 9)
gStndp<-c(16, 23, 29, 36)
smp1<-runif(number_basis*smp_num, 0.0, 1.0)
geno_expn<-matrix(smp1, smp_num, number_basis)
gchr<-c(1, 1)
gchrp<-c(3, 3, 3)
outerEpi(pheno, gstnd, gStndp, geno_expn, gname, gNamep, gchr, gchrp)
```

outerSnplListInteraction

Pairwise Interaction Test Outer The SNP Lists

Description

Test the SNP-SNP interaction. And the SNPs are organized into two different SNP Lists.

Usage

```
outerSnplListInteraction(pheno, snplList1, snplList2)
```

Arguments

pheno	Vector of phenotype data.
snplList1	Matrix of the genotypes of all the SNPs on the first SNP list for testing the pairwise interactions.
snplList2	Matrix of the genotypes of all the SNPs on the second SNP list for testing the pairwise interactions.

Details

This function aims to test the pairwise interactions between the SNPs organized into different data structures. It takes phenotype and genotypes of the SNPs as the input. And output all the p values for the interactions of SNP pairs.

Value

Return a frame contains names of all the SNPs pairs and p values for interactions of these pairs.

Author(s)

Futao Zhang

Examples

```
snp_list_1 <- as.data.frame(matrix(round(runif(3000,0,2)),1000,3))
snp_list_2 <- as.data.frame(matrix(round(runif(5000,0,2)),1000,5))
colnames(snp_list_1 )<-c("rs10","rs11","rs12")
colnames(snp_list_2 )<-c("rs20","rs21","rs22","rs23","rs24")
pheno<- round(runif(1000,40,60))
outerSnpListInteraction(pheno,snp_list_1,snp_list_2)
```

pCAInteraction

Epistasis Test by Principal Component Analysis

Description

Test the epistasis between two genes (or genomic regions) with the principal components analysis method.

Usage

```
pCAInteraction(phenoData, x_A, x_B)
```

Arguments

phenoData	Vector of phenotype data which can be quantitative trait or binary trait.
x_A	Matrix of genotype of gene A.
x_B	Matrix of genotype of gene B.

Details

This function takes phenotype vector and genotype matrices as input and tests the epistasis using PCA method. The number of principal components is determined by PCA to explain 80 percent of the genetic variation. The interaction between gene A and gene B is tested with chi-squared test.

Value

It returns the p value of chi-squared test for epistasis detection between gene A and gene B.

Author(s)

Futao Zhang

Examples

```

smp_num=1000
number_snp_A=25
number_snp_B=20
pheno<-sample(c(0:500), smp_num, replace=TRUE)
smp1=rep(0, number_snp_A*smp_num)
idx_1=sample(c(1:(number_snp_A*smp_num)), ceiling(number_snp_A*smp_num/100))
idx_2=sample(c(1:(number_snp_A*smp_num)), ceiling(number_snp_A*smp_num/200))
smp1[idx_1]=1
smp1[idx_2]=2
geno_A=matrix(smp1, smp_num, number_snp_A)

smp1=sample(c(0,1,2), number_snp_B*smp_num, replace=TRUE)
geno_B=matrix(smp1, smp_num, number_snp_B)
pCAInteraction(pheno, geno_A, geno_B)

```

pCAPionwiseEpistasis *Epistasis Test by PCA Method and Pionwise Method*

Description

This function is the another entrance of the software package. It tests the Genome Wide Epistasis by PCA Method and Pionwise Method.

Usage

```
pCAPionwiseEpistasis(wDir, oEpi, phenoInfo, gnoFiles, mapFiles, gLst, rng)
```

Arguments

wDir	The dataset directory. If the dataset is in the working directory, wDir is ".".
oEpi	Output data frame which contains all the names of gene pairs and the p values for their epistasis.
phenoInfo	It is a matrix with two columns. One column is the individual ID and the other is the phenotype. The phenotype can be quantitative trait or binary trait.
gnoFiles	The vector of genotype file names. It contains the genotype file names indicating where to read the genotype files.
mapFiles	The vector of SNP genetic map file names. It contains the map file names indicating where to read the genetic map files.
gLst	Gene annotation which includes gene name, chromosome, start position and end position.
rng	A numeric value which represents gene region extensible scope.

Details

The genotypes on different chromosome are stored in different files. The full names of these files are listed in the index file that is taken as the input parameter. After the index file is loaded, the function knows where to read the genotypes files. This function analyses the genotypes files one by another. That means this function tests the epistasis of genomic regions both of which are on the same chromosome(file), then the epistasis of genomic regions which are on different chromosomes(files).

This function can test epistasis both with PCA method and pointwise method. For a pair of genes, we assume that the total number of all possible SNP pairs is K , The minium p value for SNP-SNP interaction among the K pairs is output as the pointwise method result of the gene pair.

Value

Return a data frame which contains all the names of gene pairs and the p values of chi-square test for their epistasis.

Author(s)

Futao Zhang

Examples

```
work_dir <-paste(system.file("extdata", package="FRGEpistasis"),"/",sep="")
##read the list of genotype files
geno_files<-read.table(system.file("extdata", "list_genotype.txt", package="FRGEpistasis"))
##read the list of map files
mapFiles<-read.table(system.file("extdata", "list_map.txt", package="FRGEpistasis"))
##read the phenotype file
phenoInfo <- read.csv(system.file("extdata", "phenotype.csv", package="FRGEpistasis"),header=TRUE)
##read the gene annotation file
gLst<-read.csv(system.file("extdata", "gene.list.csv", package="FRGEpistasis"))
##define the extension scope of gene region
rng=0

##log transformation
phenoInfo [,2]=log(phenoInfo[,2])
out_epi<-data.frame()

pCAPointwiseEpistasis(work_dir,out_epi,phenoInfo,geno_files,mapFiles,gLst,rng)
```

pointwiseInteraction *Pointwise Interaction Test*

Description

Test the epistasis of the gene pair by pointwise method

Usage

```
pointwiseInteraction(phenoData, x_A, x_B)
```

Arguments

phenoData	Vector of phenotype data which can be quantitative trait or binary trait.
x_A	Matrix of genotype of gene A.
x_B	Matrix of genotype of gene B.

Details

This function takes phenotype vector and genotype matrices as input and tests the epistasis using pointwise method. For a pair of genes, we assume that the total number of all possible SNP pairs is K (one SNP from one gene and the other SNP from the other gene). The interaction of each SNP pair between the two genes is tested. The minimum p value for SNP-SNP interaction among the K pairs is output as the pointwise method result of the gene pair.

Value

Return the minimum p value for SNP-SNP interaction among the K pairs

Author(s)

Futao Zhang

Examples

```
smp_num=1000
number_snp_A=25
number_snp_B=20
pheno<-sample(c(0:500), smp_num, replace=TRUE)
smp1=rep(0, number_snp_A*smp_num)
idx_1=sample(c(1:(number_snp_A*smp_num)), ceiling(number_snp_A*smp_num/100))
idx_2=sample(c(1:(number_snp_A*smp_num)), ceiling(number_snp_A*smp_num/200))
smp1[idx_1]=1
smp1[idx_2]=2
geno_A=matrix(smp1, smp_num, number_snp_A)

smp1=sample(c(0,1,2), number_snp_B*smp_num, replace=TRUE)
geno_B=matrix(smp1, smp_num, number_snp_B)
pointwiseInteraction(pheno, geno_A, geno_B)
```

rankTransPheno

Rank-Based Inverse Normal Transformation

Description

Rank-Based Inverse Normal Transformation of Phenotype

Usage

```
rankTransPheno(pheno, para_c)
```

Arguments

pheno	Vector of phenotype which is the quantitative trait.
para_c	Adjust parameter, commonly as 0, 1/3, 3/8 or 1/2.

Details

Some variables are not normally distributed. And using statistical tests on this data can give misleading results because they do not meet the statistical assumptions. This function implements Rank-Based Inverse Normal Transformation to make phenotype normally distributed.

Value

Return vector of rank-based inverse normal transformed phenotype.

Author(s)

Futao Zhang

References

T. Mark Beasley, Stephen Erickson and David B. Allison. Rank-Based Inverse Normal Transformations are Increasingly Used, But are They Merited? *Behav Genet.* 2009 Sep.;39(5):580-595.

Examples

```
c=0.5
smp_num=100
pheno<-sample(c(0:500), smp_num, replace=TRUE)
rankTransPheno(pheno, c)
```

reduceGeno

Reduction Dimension of Genotype

Description

Reduce Dimension of Genotype using Functional Regression Model

Usage

```
reduceGeno(wDir, pheno, gnoFiles, mapFiles, gLst, rng)
```

Arguments

wDir	The dataset directory. If the dataset is in the working directory, wDir is ".".
pheno	It is a matrix with two columns. One column is the individual ID and the other is the phenotype. The phenotype can be quantitative trait or binary trait.
gnoFiles	The vector of genotype file names. It contains the genotype file names indicating where to read the genotype files.
mapFiles	The vector of SNP genetic map file names. It contains the map file names indicating where to read the genetic map files.
gLst	Gene annotation which includes gene name, chromosome, start position and end position.
rng	A numeric value which represents gene region extensible scope.

Details

This function reduces the dimension of genotypes of all the genes with Fourier expansion. In real dataset the genotypes on different chromosome are always organized into different files. And each genotype file is very large. This function processes the genotype files in turns. The reduced genotype data (the expansion data) of all the chromosomes are combined together. The expansion data and other information are organized into a list. During Fourier expansion, the physical position information of the SNPs are used. This is one of merits of our method.

Value

Return a list that includes reduced genotype data, gene names, chromosome information, start index and end index of each gene.

Author(s)

Futao Zhang

Examples

```
wDir <-paste(system.file("extdata", package="FRGEpistasis"),"/",sep="")
gnoFiles<-read.table(system.file("extdata", "list_genotype.txt", package="FRGEpistasis"))
mapFiles<-read.table(system.file("extdata", "list_map.txt", package="FRGEpistasis"))
phenoInfo <- read.csv(system.file("extdata", "phenotype.csv", package="FRGEpistasis"),header=TRUE)
gLst<-read.csv(system.file("extdata", "gene.list.csv", package="FRGEpistasis"))
rng=0
gInfo=reduceGeno(wDir,phenoInfo,gnoFiles,mapFiles,gLst,rng)
```

snpPairInteraction *SNP-SNP interaction*

Description

Test the interaction of one SNP with another

Usage

```
snpPairInteraction(pheno, snp1, snp2)
```

Arguments

pheno	Vector of phenotype data which can be quantitative trait or binary trait.
snp1	Vector of genotype data of SNP1.
snp2	Vector of genotype data of SNP2.

Details

This function tests the interaction of one SNP with another.

Value

Return the p value for snp-snp interaction

Author(s)

Futao Zhang

Examples

```
pheno<- round(runif(1000,40,60))
snp1<-round(runif(1000,0,2))
snp2<-round(runif(1000,0,2))
pval=snpPairInteraction(pheno,snp1,snp2)
```

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