

# Package ‘velociraptor’

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**Title** Toolkit for Single-Cell Velocity

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**Description** This package provides Bioconductor-friendly wrappers for RNA velocity calculations in single-cell RNA-seq data. We use the basilisk package to manage Conda environments, and the zellkonverter package to convert data structures between SingleCellExperiment (R) and AnnData (Python). The information produced by the velocity methods is stored in the various components of the SingleCellExperiment class.

**Depends** SummarizedExperiment

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**BugReports** <https://github.com/kevinrue/velociraptor/issues>

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**Author** Kevin Rue-Albrecht [aut, cre] (<<https://orcid.org/0000-0003-3899-3872>>),  
 Aaron Lun [aut] (<<https://orcid.org/0000-0002-3564-4813>>),  
 Charlotte Soneson [aut] (<<https://orcid.org/0000-0003-3833-2169>>),  
 Michael Stadler [aut] (<<https://orcid.org/0000-0002-2269-4934>>)

**Maintainer** Kevin Rue-Albrecht <kevinrue67@gmail.com>

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embedVelocity	<i>Project velocities onto an embedding</i>
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### Description

Project the velocity vector for each cell onto an existing low-dimensional embedding.

### Usage

```
embedVelocity(x, vobj, ...)

## S4 method for signature 'ANY'
embedVelocity(x, vobj, ...)

## S4 method for signature 'SingleCellExperiment'
embedVelocity(x, vobj, ..., use.dimred = 1)
```

### Arguments

x	A numeric matrix of low-dimensional coordinates, e.g., after t-SNE. Alternatively, a <a href="#">SingleCellExperiment</a> containing such coordinates in its <a href="#">reducedDims</a> .
vobj	A <a href="#">SingleCellExperiment</a> containing the output of the velocity calculations, typically after running <a href="#">scvelo</a> .
...	For the generic, further arguments to pass to specific methods. For the ANY method, further arguments to pass to the <code>velocity_embedding</code> Python function from <a href="#">scVelo</a> . For the <code>SingleCellExperiment</code> method, further arguments to pass to the ANY method.
use.dimred	String or integer scalar specifying the reduced dimensions to retrieve from x.

**Details**

This is a simple wrapper around the `scvelo.tools.velocity_embedding` function. Briefly, we construct a cell-cell transition matrix where a cell is more likely to transition to one of its neighbors if its velocity vector is pointing in the same direction as that neighbor. The resulting matrix is then used to compute a weighted average of the positions in `x`, allowing us to compute a velocity in the low-dimensional embedding.

**Value**

A numeric matrix of the same dimensions as `x`, containing the projected velocity vectors in that embedding.

**Author(s)**

Aaron Lun

**Examples**

```
example(scvelo, echo=FALSE) # recycling that example.

# Making up a new embedding.
tsne.results <- matrix(rnorm(2*ncol(out)), ncol=2)

# Projecting the future state of each cell:
projected <- embedVelocity(tsne.results, out)
```

---

gridVectors

*Summarize vectors into a grid*

---

**Description**

Summarize the velocity vectors into a grid, usually for easy plotting.

**Usage**

```
gridVectors(x, embedded, ...)

## S4 method for signature 'ANY'
gridVectors(
  x,
  embedded,
  resolution = 40,
  scale = TRUE,
  as.data.frame = TRUE,
  return.intermediates = FALSE
)
```

```
## S4 method for signature 'SingleCellExperiment'
gridVectors(x, embedded, ..., use.dimred = 1)
```

### Arguments

<code>x</code>	A numeric matrix of low-dimensional coordinates, e.g., after t-SNE. Alternatively, a <code>SingleCellExperiment</code> containing such coordinates in its <code>reducedDims</code> .
<code>embedded</code>	A low-dimensional projection of the velocity vectors into the embedding of <code>x</code> . This should be of the same dimensions as <code>x</code> and is typically produced by <code>embedVelocity</code> .
<code>...</code>	For the generic, further arguments to pass to specific methods. For the <code>SingleCellExperiment</code> method, further arguments to pass to the ANY method.
<code>resolution</code>	Integer scalar specifying the resolution of the grid, in terms of the number of grid intervals along each axis.
<code>scale</code>	Logical scalar indicating whether the averaged vectors should be scaled by the grid resolution.
<code>as.data.frame</code>	Logical scalar indicating whether the output should be a <code>data.frame</code> . If <code>FALSE</code> , a list of two matrices is returned.
<code>return.intermediates</code>	Logical scalar indicating whether intermediate objects should also be returned. This enforces <code>as.data.frame=FALSE</code> and throws a warning if it is <code>TRUE</code> .
<code>use.dimred</code>	String or integer scalar specifying the reduced dimensions to retrieve from <code>x</code> .

### Details

This partitions the bounding box of `x` into a grid with `resolution` units in each dimension. The locations and vectors of all cells in each block are averaged to obtain a representative of that block. This is most obviously useful for visualization to avoid overplotting of velocity vectors.

If `scale=TRUE`, per-block vectors are scaled so that the median vector length is comparable to the spacing between blocks. This improves visualization when the scales of `x` and `embedded` are not immediately comparable.

### Value

If `as.data.frame=FALSE`, a list is returned containing `start` and `end`, two numeric matrices with one row per non-empty block in the grid and one column per column in `x`. `start` contains the mean location of all cells inside that block, and `end` contains the endpoint after adding the (scaled) average of the block's cell's velocity vectors.

If `as.data.frame=TRUE`, a `data.frame` is returned with numeric columns of the same contents as the list above. Column names are prefixed by `start.*` and `end.*`.

If `return.intermediates=TRUE`, a list is returned (irrespective of the value of `as.data.frame`) that in addition to `start` and `end` also contains intermediate objects `limits` (the ranges in `x` and `y`), `delta` (the grid intervals in `x` and `y`), `categories` (a `DataFrame` with integer row and column indices for each cell that specify the grid field that it is contained in), `grp` (numerical index of grid fields for each cell) and `vec` (velocity vectors for non-empty grid fields).

**Author(s)**

Aaron Lun

**See Also**[embedVelocity](#), to generate embedded.**Examples**

```
tsne.results <- matrix(rnorm(10000), ncol=2)
tsne.vectors <- matrix(rnorm(10000), ncol=2)

out <- gridVectors(tsne.results, tsne.vectors)

# Demonstration for plotting.
plot(tsne.results[,1], tsne.results[,2], col='grey')
arrows(out$start.1, out$start.2, out$end.1, out$end.2, length=0.05)
```

plotVelocity

*Phase and velocity graphs for a set of genes***Description**

For a each gene in a set of genes, show the phase graph (spliced versus unspliced counts and fitted model) and reduced dimension graphs with cell colored by velocity and (spliced) expression.

**Usage**

```
plotVelocity(
  x,
  genes,
  use.dimred = 1,
  assay.splicedM = "Ms",
  assay.unsplicedM = "Mu",
  which.plots = c("phase", "velocity", "expression"),
  genes.per.row = 1,
  color_by = "#222222",
  color.alpha = 0.4,
  colors.velocity = c("#A50026", "#D73027", "#F46D43", "#FDAE61", "#FEE08B", "#FFFFBF",
    "#D9EF8B", "#A6D96A", "#66BD63", "#1A9850", "#006837"),
  colors.expression = c("#440154", "#482576", "#414487", "#35608D", "#2A788E",
    "#21908C", "#22A884", "#43BF71", "#7AD151", "#BBD227", "#FDE725"),
  max.abs.velo = 0.001
)
```

**Arguments**

<code>x</code>	A <a href="#">SingleCellExperiment</a> object with RNA velocity results as returned by <a href="#">scvelo</a> , and low-dimensional coordinates, e.g., after t-SNE, in its <a href="#">reducedDims</a> .
<code>genes</code>	A character vector with one or several genes for which to plot phase and velocity graphs. <code>genes</code> have to be in <code>rownames(x)</code> .
<code>use.dimred</code>	String or integer scalar specifying the reduced dimensions to retrieve from <code>x</code> .
<code>assay.splicedM</code>	An integer scalar or string specifying the assay of <code>x</code> containing the moments of spliced abundances.
<code>assay.unsplicedM</code>	An integer scalar or string specifying the assay of <code>x</code> containing the moments unspliced abundances.
<code>which.plots</code>	A character vector specifying which plots to create for each gene. Possible values are "phase", "velocity", "expression" and correspond to the phase graph or reduced dimension graphs with cells colored by velocity or (spliced) expression.
<code>genes.per.row</code>	An integer scalar with the numbers of genes to visualize per row of plots. For example, if <code>which.plots = c("phase", "expression")</code> and <code>genes.per.row = 2</code> , the resulting figure will have four plot panels per row.
<code>color_by</code>	A character scalar specifying a column in <code>colData(x)</code> to color cells in the phase graph. Alternatively, <code>color_by</code> can be set to vector of valid R colors, either of length one (recycled for all cells) or of length <code>ncol(x)</code> , which will then be used to color cells in the phase graph.
<code>color.alpha</code>	An integer scalar giving the transparency of colored cells. Possible values are between 0 (fully transparent) and 1.0 (opaque).
<code>colors.velocity</code> , <code>colors.expression</code>	Character vectors specifying the color ranges used for mapping velocities and expression values. The defaults are <code>RColorBrewer::brewer.pal(11, "RdYlGn")</code> for the velocities and <code>viridisLite::viridis(11)</code> for the expression values.
<code>max.abs.velo</code>	A numeric scalar greater than zero giving the maximum absolute velocity to limit the color scale for the "velocity" graph.

**Details**

Please note that `plotVelocity` will modify parameters of the current graphics device using [layout](#) and [par](#), in order to create the layout for the generated graph panels.

**Value**

A patchwork object with the plots selected by `which.plot` for the genes in `genes`, arranged in a grid according to `genes.per.row`.

**Author(s)**

Michael Stadler

### See Also

[scvelo](#), to generate x, [brewer.pal](#) and [viridis](#) for creation of color palettes, packages **ggplot2** and **patchwork** used to generate and arrange the plots.

### Examples

```
library(scuttle)
set.seed(42)
sce1 <- mockSCE(ncells = 100, ngenes = 500)
sce2 <- mockSCE(ncells = 100, ngenes = 500)

datlist <- list(X=counts(sce1), spliced=counts(sce1), unspliced=counts(sce2))

out1 <- scvelo(datlist, mode = "steady_state")
out2 <- scvelo(datlist, mode = "dynamical")

plotVelocity(out1, c("Gene_0031", "Gene_0268"))
plotVelocity(out2, c("Gene_0031", "Gene_0268"))
```

---

plotVelocityStream      *Velocity stream plot in low-dimensional space*

---

### Description

Plot velocities embedded into low-dimensional space as a stream plot. Stream lines are lines that follow the gradient in the velocity field and illustrate paths that cells could follow based on observed RNA velocities.

### Usage

```
plotVelocityStream(
  sce,
  embedded,
  use.dimred = 1,
  color_by = "#444444",
  color.alpha = 0.2,
  grid.resolution = 60,
  scale = TRUE,
  stream.L = 10,
  stream.min.L = 0,
  stream.res = 4,
  stream.width = 8,
  color.streamlines = FALSE,
  color.streamlines.map = c("#440154", "#482576", "#414487", "#35608D", "#2A788E",
    "#21908C", "#22A884", "#43BF71", "#7AD151", "#BBDF27", "#FDE725"),
  arrow.angle = 8,
  arrow.length = 0.8
)
```

**Arguments**

sce	A <a href="#">SingleCellExperiment</a> object containing low-dimensional coordinates, e.g., after t-SNE, in its <a href="#">reducedDims</a> .
embedded	A low-dimensional projection of the velocity vectors into the embedding of sce. This should be of the same dimensions as sce and is typically produced by <a href="#">embedVelocity</a> .
use.dimred	String or integer scalar specifying the reduced dimensions to retrieve from sce.
color_by	A character scalar specifying a column in <code>colData(sce)</code> to color cells in the phase graph. Alternatively, <code>color_by</code> can be set to a valid R color to be used to color cells.
color.alpha	An integer scalar giving the transparency of colored cells. Possible values are between 0 (fully transparent) and 1.0 (opaque).
grid.resolution	Integer scalar specifying the resolution of the grid, in terms of the number of grid intervals along each axis.
scale	Logical scalar indicating whether the averaged vectors should be scaled by the grid resolution.
stream.L	Integer scalar giving the typical length of a streamline low-dimensional space units.
stream.min.L	A numeric scalar with the minimum length of segments to be shown.
stream.res	Numeric scalar specifying the resolution of estimated streamlines (higher numbers increase smoothness of lines but also the time for computation).
stream.width	A numeric scalar controlling the width of streamlines.
color.streamlines	Logical scalar. If TRUE streamlines will be colored by local velocity. Arrows cannot be shown in that case.
color.streamlines.map	A character vector specifying the color range used for mapping local velocities to streamline colors. The default is <code>viridisLite::viridis(11)</code> .
arrow.angle, arrow.length	Numeric scalars giving the angle and length of arrowheads.

**Details**

`grid.resolution` and `scale` are passed to [gridVectors](#), which is used to summarize the velocity vectors into an initial grid. A full regular grid is computed from that and used in [geom\\_streamline](#) to calculate streamlines. The following arguments are passed to the arguments given in parenthesis of [geom\\_streamline](#): `stream.L` (`L`), `stream.res` (`res`), `stream.min.L` (`min.L`), `arrow.angle` (`arrow.angle`) and `arrow.length` (`arrow.length`). Streamlines are computed by simple integration with a forward Euler method, and `stream.L` and `stream.res` are used to compute the number of steps and the time interval between steps for the integration. `stream.width` is multiplied with `..step..` estimated by [geom\\_streamline](#) to control the width of streamlines.

**Value**

A `ggplot2` object with the streamline plot.



**Author(s)**

Michael Stadler

**See Also**

[gridVectors](#) used to summarize velocity vectors into a grid (velocity field), the **ggplot2** package used for plotting, [geom\\_streamline](#) in package **metR** used to calculate and add streamlines from the RNA velocity field to the plot, [viridis](#) for creation of color palettes.

**Examples**

```
library(scuttle)
set.seed(42)
sce1 <- mockSCE(ncells = 100, ngenes = 500)
sce2 <- mockSCE(ncells = 100, ngenes = 500)

datlist <- list(X=counts(sce1), spliced=counts(sce1), unspliced=counts(sce2))

out <- scvelo(datlist, mode = "dynamical")

em <- embedVelocity(reducedDim(out, 1), out)[,1:2]

plotVelocityStream(out, em)
plotVelocityStream(out, em, color.streamlines = TRUE)
```

---

scvelo

*RNA velocity with scVelo*

---

**Description**

Perform RNA velocity calculations with the **scVelo** package.

**Usage**

```
scvelo(x, ...)

## S4 method for signature 'ANY'
scvelo(
  x,
  subset.row = NULL,
  sf.X = NULL,
  sf.spliced = NULL,
  sf.unspliced = NULL,
  use.theirs = FALSE,
  mode = c("steady_state", "deterministic", "stochastic", "dynamical"),
  scvelo.params = list(),
  dimred = NULL,
```

```

    ncomponents = 30,
    BPPARAM = SerialParam(),
    BSPARAM = bsparam()
)

## S4 method for signature 'SummarizedExperiment'
scvelo(
  x,
  ...,
  assay.X = "counts",
  assay.spliced = "spliced",
  assay.unspliced = "unspliced"
)

## S4 method for signature 'SingleCellExperiment'
scvelo(x, ..., sf.X = sizeFactors(x), dimred = NULL, use.dimred = NULL)

```

## Arguments

<code>x</code>	A named list of three matrices of the same dimensions where genes are in rows and cells are in columns. The list should contain "spliced" and "unspliced" entries containing spliced and unspliced counts, respectively. It should also contain an "X" entry containing the "usual" count matrix, see details below. Alternatively, a <a href="#">SummarizedExperiment</a> object containing three such matrices among its assays.
<code>...</code>	For the generic, further arguments to pass to specific methods. For the <a href="#">SummarizedExperiment</a> and <a href="#">SingleCellExperiment</a> methods, further arguments to pass to the ANY method.
<code>subset.row</code>	A character, integer or logical vector specifying the genes to use for the velocity calculations. Defaults to all genes.
<code>sf.X</code>	A numeric vector containing size factors for usual count matrix. Defaults to <a href="#">librarySizeFactors</a> on the "X" matrix in <code>x</code> .
<code>sf.spliced</code>	A numeric vector containing size factors for the spliced counts for each cell. Defaults to <a href="#">librarySizeFactors</a> on the "spliced" matrix in <code>x</code> .
<code>sf.unspliced</code>	A numeric vector containing size factors for the unspliced counts for each cell. Defaults to <a href="#">librarySizeFactors</a> on the "unspliced" matrix in <code>x</code> .
<code>use.theirs</code>	Logical scalar indicating whether <b>scVelo</b> 's gene filtering and normalization should be used.
<code>mode</code>	String specifying the method to use to estimate the transcriptional dynamics.
<code>scvelo.params</code>	List of lists containing arguments for individual <b>scVelo</b> functions, see details below.
<code>dimred</code>	A low-dimensional representation of the cells with number of rows equal to the number of cells in <code>x</code> , used to find the nearest neighbors.
<code>ncomponents</code>	Numeric scalar indicating the number of principal components to obtain. Only used if <code>use.theirs=FALSE</code> and <code>dimred=NULL</code> .

BPPARAM	A <a href="#">BiocParallelParam</a> object specifying whether the PCA calculations should be parallelized. Only used if <code>use.theirs=FALSE</code> and <code>dimred=NULL</code> .
BSPARAM	A <a href="#">BiocSingularParam</a> object specifying which algorithm should be used to perform the PCA. Only used if <code>use.theirs=FALSE</code> and <code>dimred=NULL</code> .
<code>assay.X</code>	An integer scalar or string specifying the assay of <code>x</code> containing the usual count matrix.
<code>assay.spliced</code>	An integer scalar or string specifying the assay of <code>x</code> containing the spliced counts.
<code>assay.unspliced</code>	An integer scalar or string specifying the assay of <code>x</code> containing the unspliced counts.
<code>use.dimred</code>	String naming the entry of <code>reducedDims(x)</code> to use for nearest neighbor calculations. Ignored if <code>dimred</code> is supplied.

## Details

This function uses the **scVelo** Python package (<https://pypi.org/project/scvelo/>) for RNA velocity calculations. The main difference from the original **velocity** approach is that the dynamical model of **scVelo** does not rely on the presence of observed steady-state populations, which should improve the reliability of the velocity calculations in general applications.

For consistency with other Bioconductor workflows, we perform as many standard steps in R as we can before starting the velocity calculations with **scVelo**. This involves:

1. Size factor-based normalization with `sf.*` values and [normalizeCounts](#). For "X", log-transformation is performed as well, while for the others, only scaling normalization is performed.
2. Subsetting all matrices to `subset.row`, most typically to a subset of interest, e.g., highly variable genes. Note that, if set, any subsetting is done *after* normalization so that library sizes are correctly computed.
3. If `dimred=NULL`, the PCA step on the log-expression values derived from the "X" matrix, using the specified `BSPARAM` to obtain the first `ncomponents` PCs.

This allows us to guarantee that, for example, the log-expression matrix of HVGs or the PCA coordinates are the same as that used in other applications like clustering or trajectory reconstruction.

Nonetheless, one can set `use.theirs=TRUE` to directly use the entire **scVelo** normalization and filtering pipeline. This ignores all of the size factors arguments (`sf.*`), all of the PCA-related arguments (`ncomponents`, `BSPARAM`) and `subset.row`. However, if a low-dimensionality result is supplied via `dimred` or `use.dimred`, the **scVelo** PCA will always be omitted.

Upon first use, this function will instantiate a conda environment containing the **scVelo** package. This is done via the **basilisk** package - see the documentation for that package for trouble-shooting.

## Value

A [SingleCellExperiment](#) is returned containing the output of the velocity calculations. Of particular interest are:

- the `velocity_pseudotime` field in the `colData`, containing the velocity pseudotime for each cell.

- the `velocity` entry of the `assays`, containing the velocity vectors for each cell.

The output will always have number of columns equal to the number of cells supplied in `x`, though the number of rows will depend on whether any subsetting (if `subset.row` is supplied) or feature selection (if `use.theirs=TRUE`) was performed.

### Comments on the three matrices

Strictly speaking, only the spliced and unspliced matrices are necessary for the velocity calculations. However, it is often the case that the spliced matrix is not actually the same as a “usual” count matrix (e.g., generated by summing counts across all exons for all mapped genes). This is due to differences in the handling of ambiguous reads that map across exon-intron boundaries, or to genomic regions that can be either exonic or intronic depending on the isoform; the spliced count matrix is more likely to exclude such reads.

We request the usual count matrix as the “`X`” entry of `x` to ensure that the PCA and nearest neighbor detection in **scVelo** are done on the same data as that used in other steps of the large analysis (e.g., clustering, visualization, trajectory reconstruction). In practice, if the usual count matrix is not available, one can often achieve satisfactory results by simply re-using the spliced count matrix as both the “`X`” and “`spliced`” entries of `x`.

Note that if reduced dimensions are supplied in `dimred`, any “`X`” entry is only used to create the `AnnData` object and is not used in any actual calculations.

### Additional arguments to Python

Additional arguments to **scVelo** functions are provided via `scvelo.params`. This is a named list where each entry is named after a function and is itself a named list of arguments for that function. The following function names are currently recognized:

- “`filter_and_normalize`”, for gene selection and normalization. This is not used unless `use.theirs=TRUE`.
- “`moments`”, for PCA and nearest neighbor detection. The PCA is not performed if `dimred` or `use.dimred` is already supplied.
- “`recover_dynamics`”
- “`velocity`”
- “`velocity_graph`”
- “`velocity_pseudotime`”
- “`latent_time`”
- “`velocity_confidence`”

See the **scVelo** documentation for more details about the available arguments.

### Author(s)

Aaron Lun, Charlotte Soneson

### References

Bergen, V., Lange, M., Peidli, S. et al. Generalizing RNA velocity to transient cell states through dynamical modeling. *Nat Biotechnol* 38, 1408–1414 (2020). <https://doi.org/10.1038/s41587-020-0591-3>

**Examples**

```
# Using mock data to demonstrate the process:
library(scuttle)
sce1 <- mockSCE()
sce2 <- mockSCE()

spliced <- counts(sce1)
unspliced <- counts(sce2)

out <- scvelo(list(X=spliced, spliced=spliced, unspliced=unspliced))
```

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